THIRUVALLUVARUNIVERSITY SERKKADU VELLORE- 632115

M.Sc. Mathematics –2022-2023 onwards

Programme Objectives:

- 1. Developthestudentwithcriticalthinkingandanalyticskills.
- 2. Enhancetheknowledgeofstudentsforpursuinghigherstudies.
- 3. Providein-depthknowledgetodesignthemathematicalmodelsinreallifeproblems.
- 4. Expertise the students to excel in their professional career.
- 5. Provide the students to understand the mathematical concepts visually.

ProgrammeEducationalObjectives:

- 1. ProvideastrongfoundationinpureandappliedMathematics.
- 2. Motivatethestudentstopursuehigherstudies.
- 3. Preparethestudentstoworkeffectivelyina group orindividually.
- 4. Enrichthestudenttofollowtheethicalandprofessionalvaluestoservethecommunity.
- 5. Encouragethestudentforlifelonglearning.

Programme Specific Outcomes:

- 1. UnderstandthetheoreticalknowledgeofMathematicalconcepts.
- 2. Developtheproblemssolvingskills.
- 3. Collaborate with the multi-disciplinary areas.
- 4. CreativelyapplyingtheknowledgeofMathematicsinselectedreallifesituations.
- 5. Appreciate the emphasis given on teaching the mathematical concepts through counterexa mples.
- 6. Gettheknowledgeofinter-disciplinaryapproach oflearning.
- 7. DeveloptheskilltosolveproblemswhichappearinthevariousexaminationslikeCSIR-NET,SET,IAS, etc
- 8. Inculcate the creative and develop research level thinking in the field of pure and applied Ma the matics.
- 9. Encouragetogo forhigherlearninginresearch.
- 10. Understandtheethicalvaluesandhumanvaluestoappreciatetheculturaldiversityandpro motethesocial harmony.

Programme Outcomes:

- 1. Acquirein-depthknowledgeofMathematicsboth intheoryandapplication.
- 2. Identifymathematicalandcomputationalmethodsinordertosolvecomprehensiveproble ms.
- 3. Recognize the various specialized areas of advanced mathematics and its applications.
- 4. Analyzeandinterpretdatatocreateanddesignnewknowledgefor complexproblems.
- $5. \ Develop the mathematical models for the applications of mathematics in real life situations.$
- 6. Exhibitthepotentialtoeffectivelyaccomplishtasksindependentlyandasamemberorlead erindiverseteams, and in multidisciplinary settings.
- 7. Developtheskillstocrackthevariouscompetitiveexamination.
- 8. Abilitytoengageinlife-longlearninginthecontextoftherapiddevelopmentsinthefield.
- 9. Demonstrate the ability towrited is sertations, reports, make effective presentations and do cumentation.
- 10. Commitmenttoprofessionalethicsandsocialresponsibilities.

THIRUVALLUVARUNIVERSITY MASTEROFSCIENCE

(Witheffectfrom2022–2023)

The Course of Study and the Scheme of Examination

@CompulsoryCourses don'tchangethiscategory. Number ofcore papers &Practicalmaybe changed

Study Com	ponents	ins.			Ma:	ximum M	arks
Course	Title	hrs / week	Creatt	Tuie of the Paper	CIA	Uni.	Total
SE	MESTER	I			• mi	Exam	10000
		6	5	Algebra-I	25	75	100
Core		6	5	Real Analysis –I	25	75	100
		6	4	Ordinary Differential Equations	25	75	100
	I	nternal E	lective fo	r same major students (Choose any one)			
@ Com				A. Probability Theory			
@ Core Flective	Paper-1	6	3	B. Mechanics	25	75	100
Elective				C. Graph Theory			
External Elective for		for other	major students (Inter/multi disciplinary pa	pers)			
@ Onen				A. Basic Mathematics	25	75	100
@ OpenPaper-16Elective6		3	B. Mathematical Foundations				
Elective Tuper 1				C. Mathematical Modeling			
30 20		20					
SEI	MESTER I	I			CIA	Uni.	Total
SEMESTER II					Exam	10101	
		6	5	Algebra-II	25	<i>Exam</i> 75	100
Core		6 6	5 5	Algebra-II Real Analysis –II	25 25	<i>Exam</i> 75 75	100 100
Core		6 6 6	5 5 4	Algebra-II Real Analysis –II Partial Differential Equations	25 25 25 25	<i>Exam</i> 75 75 75	100 100 100 100
Core	I	6 6 6 nternal E	5 5 4 lective fo	Algebra-II Real Analysis –II Partial Differential Equations r same major students (Choose any one)	25 25 25	<i>Exam</i> 75 75 75	100 100 100 100
Core		6 6 nternal E	5 5 4 lective fo	Algebra-II Real Analysis –II Partial Differential Equations r same major students (Choose any one) A.Mathematical Statistics	25 25 25	<i>Exam</i> 75 75 75	100 100 100 100
Core @ Core	I Paper-2	6 6 nternal E 5	5 5 4 lective fo	Algebra-II Real Analysis –II Partial Differential Equations or same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory	25 25 25 25 25	<i>Exam</i> 75 75 75 75	100 100 100 100 100 100
Core @ Core Elective	I Paper-2	6 6 nternal E 5	5 5 4 lective fo	Algebra-II Real Analysis –II Partial Differential Equations r same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations	25 25 25 25 25	Exam 75 75 75 75 75	100 100 100 100 100 100
Core @ Core Elective	I Paper-2 External	6 6 nternal E 5 Elective	5 5 4 lective fo 3	Algebra-II Real Analysis –II Partial Differential Equations or same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations major students (Inter/multi disciplinary pa	25 25 25 25 25 25 25	Exam 75 75 75 75 75	100 100 100 100 100 100
Core @ Core Elective	I Paper-2 External	6 6 nternal E 5 Elective 5	5 5 4 lective fo 3 for other 3	Algebra-II Real Analysis –II Partial Differential Equations r same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations major students (Inter/multi disciplinary pa A. Fundamentals of Insurance	25 25 25 25 25 25 25	Exam 75 75 75 75 75	100 100 100 100 100
© Core Elective	I Paper-2 External Paper-2	6 6 nternal E 5 Elective 5	5 5 4 lective fo 3 for other 3	Algebra-II Real Analysis –II Partial Differential Equations or same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations major students (Inter/multi disciplinary particular) A. Fundamentals of Insurance B. Numerical Methods	25 25 25 25 25 25 25 25 25 25	Exam 75 75 75 75 75 75	100 100 100 100 100 100
© Core © Core Elective © Open Elective	I Paper-2 External Paper-2	6 6 nternal E 5 Elective 5	54lective for3for other3	Algebra-II Real Analysis –II Partial Differential Equations r same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations major students (Inter/multi disciplinary path) A. Fundamentals of Insurance B. Numerical Methods C. Fundamentals of Business Statistics	25 25 25 25 25 25 25 25 25	Exam 75 75 75 75 75 75	100 100 100 100 100 100
© Core © Core Elective © Open Elective © Compulso	I Paper-2 External Paper-2 ory Paper	6 6 nternal E 5 Elective 5 2	5 5 4 lective fo 3 for other 3 2	Algebra-II Real Analysis –II Partial Differential Equations or same major students (Choose any one) A.Mathematical Statistics B. Fuzzy Set Theory C. Difference Equations major students (Inter/multi disciplinary particulation) A. Fundamentals of Insurance B. Numerical Methods C. Fundamentals of Business Statistics Human Rights & Duties	25 25 25 25 25 25 25 25 25	Exam 75 75 75 75 75 75 75	100 100 100 100 100 100 100 100
	Study Components Course Title Core Image: Core Elective Image: Core Elective Image: Core Elective Paper-1 Image: Core Elective Image: Core Elective Image: Core Elective Paper-1	Study Components ins. hrs / week Course Title hrs / week SEWESTER I 6 Core 6 Image:	Study Components ins. hrs / week Credit Course Title hrs / week Credit SEWESTER I 6 5 Core 6 5 Core 6 5 Core 6 4 Core 6 4 Core 6 3 Paper-1 6 3 Copen Paper-1 6 3 Paper-1 30 20 3	Study Componentsins. hrs / weekCreditTitle of the PaperCourse TitleSEMESTER ICore65Algebra-ICore65Real Analysis –ICore64Ordinary Differential EquationsCore64Ordinary Differential EquationsCore64Ordinary Differential EquationsCorePaper-163Paper-163A. Probability TheoryElectiveFaper-163Paper-163B. Mechanics C. Graph Theory@ Open ElectivePaper-163Basic Mathematical Foundations C. Mathematical FoundationsC. Mathematical ModelingImage: Set of the Paper I3020	Study Components ins. hrs / week Credit Title of the Paper Max Course Title week Credit Title of the Paper CIA SEWESTER I CIA CIA Core 6 5 Algebra-I 25 Core 6 5 Real Analysis –I 25 Core 6 4 Ordinary Differential Equations 25 Core Faper-1 6 3 A. Probability Theory 25 Core Paper-1 6 3 B. Mechanics 25 Core Paper-1 6 3 B. Machanics 25 Core Paper-1 6 3 B. Machanics 25 Core Paper-1 6 3 B. Machanics 25 Core Paper-1 6 3 B. Mathematical Foundations 25 Core 30 20 Internatical Modeling Internatical Modeling Internatical Modeling	Study Componentsins. hrs / weekCredit veekTitle of the Paper $M = M = M = M = M = M = M = M = M = M =$	

Sl.	Study Com	ponents	ins.	Credit	Title of the Denor	Max	ximum M	arks
No.	Course	Title	nrs / week	Creau	Tute of the Faper	~~ (Uni.	
	SEN	IESTER II	[CIA	Exam	Total
			6	6	Complex Analysis –I	25	75	100
	Core		6	5	Topology	25	75	100
			6	5	Differential Geometry	25	75	100
		In	ternal El	ective for	r same major students (Choose any one)			
	@ Core Elective	Paper-3	6	3	A. LaTeX B. Discrete Mathematics C. Operations Research	25	75	100
		External	Elective	for other	major students (Inter/multi disciplinary pap	ers)		
	@ Open Elective	Paper-3	6	3	A. Mathematical Biology B. Quantitative Techniques C. SCILAB	25	75	100
	@MOOC Courses		-	2				
	@Field Study			2		100		100
			30	26				
	SEN	IESTER IV	7			CIA	Uni. Exam	Total
	Core		5	4	Complex Analysis –II	25	75	100
			5	4	Fluid Dynamics	25	75	100
			5	5	Functional Analysis	25	75	100
	@ Core	Project Compulsory	5	5	Project with viva voce	10 (75 P) +25)0 roject viva)	100
		In	ternal El	ective for	r same major students (Choose any one)			
	@Core Elective	Paper-4	5	3	A. Number Theory and CryptographyB. Advanced Numerical AnalysisC. Calculus of Variations and IntegralEquations	25	75	100
		External	Elective	for other	major students (Inter/multi disciplinary pap	pers)		
	@ Open Elective (Non-Major)	Paper-4	5	3	A. Mathematical Economics B.Entrepreneurial Development C. Programming in C++	25	75	100
			30 120	24 92				

Semester : I

Paper code :

Paper type : Core Name of the Paper : Algebra-I Credit : 5

Hours of Teaching:90 hrs

Course Objectives:

The objective of this course are to:

- 1. Study and develop the concept of group action and learn Sylow's theorem and its applications.
- 2. Introducing structure theorem on abelian group and studying its applications.
- 3. Get the knowledge on algebraic structure Modules and its properties
- 4. Understand canonical forms of linear transformations.
- 5. Demonstrate insight into Linear algebra with focus on properties of matrix of transformations.

Course Outcomes:

After successful completion on the course the student will be able to

- **CO1** Demonstrate ability to think group actions critically by Cayley's theorem and apply the Sylow's theorems to describe the structure of certain finite abelian groups
- **CO2** Understand the concept of the internal and external direct product of groups. Also, apply the structure theorem on abelian groups to find the non-isomorphic abelian groups of certain orders.
- CO3 Check the irreducibility of given polynomial in the defined Field
- CO4 Know about Module and, difference between the Algebraic structures, Vector space and Module.
- **CO5** Acquire the knowledge of the Linear transformation in canonical forms. Also, the matrix form of linear transformation and its properties.

1

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes No		Yes	No
2	Yes	Yes	No	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Matching Table:

Unit – 1 Group Theory

Another counting principle - class equation for finite groups and its applications - Sylow's theorems (For theorem 2.12.1, Only First proof)

18 hours

18 hours

18 hours

Chapter 2: Sections 2.11 and 2.12

Unit - 2Group Theory (Continuation)18 hours

Direct products - Finite abelian groups

Chapter 2: Sections 2.13 and 2.14 (Only Theorem 2.14.1))

Unit – 3 Ring Theory

Polynomial Rings – Polynomials over the Rational Field

Chapter 3: Sections 3.9 to 3.10

Unit – 4 Modules and Linear Transformations

Modules –LinearTransformations: Nilpotent transformations - Jordan form - rational canonical form.

Chapter 4: Section 4.5

Chapter 6: Sections 6.5to 6.7

Unit - 5Linear Transformations18 hours

Hermitian, unitary, normal transformations, real quadratic form.

Chapter 6: Sections 6.10 and 6.11

Text book:

I.N. Herstein, Topics in Algebra, 2nd Edition. Wiley.1975

2

Reference Books:

- 1. D.S.Dummit and R.M.Foote. Abstract Algebra. Wiley 2003
- 2. M. Artin, Algebra, Prentice Hall of India, 1991
- 3. J.A. Gallian. Contemporary Abstract Algebra. 4th Edition. Narosa Publishing 2011
- 4. P.B.Battacharya, S.K.Jain, and S.R.Nagpaul, Basic Abstract Algebra(II Edition) Cambridge University Press, 1997.(Indian Edition)
- 5. I.S. Luther and I.B.S. Passi, Algebra, Vol.I Groups(1996), Vol. II Rings, Narosa Publishing House, New Delhi, 1999.
- 6. L. Smith, Linear transformation: Example and Applications. In: Linear Algebra, Undergraduate texts in Mathematics, Springer, New york. NY, 1998.

E-Materials:

https://nptel.ac.in/courses/111108098/

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	Μ	S	Μ	S	S	S
CO2	S	S	Μ	Μ	Μ	S	Μ	S	S	S
CO3	S	S	Μ	Μ	S	S	Μ	S	S	S
CO4	S	S	Μ	Μ	S	S	Μ	S	S	S
CO5	S	S	Μ	Μ	S	S	Μ	S	S	S

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : I

Paper code :

Paper type : Core

Credit : 5

Name of the Paper : RealAnalysis– I

Hours of Teaching:90 hrs

CourseObjectives:

Theobjectives of the courseis to

- 1. Workcomfortablywithfunctionsofbounded variation
- 2. StudytheRiemann-StieltjesIntegration
- 3. Expertise the students to excel in integration under integral sign.
- 4. Get the knowledge about the convergence of infinite series, infinite product and uniform convergence and its interplay between various limiting operations.
- 5. Provide the students to understands uniform convergence and continuity of functions.

Course Outcomes:

After successful completion on the course the student will be able to

- CO1 Understandtheconceptoffunctionsofboundedvariation.
- CO2 Acquires knowledge on Riemann Stieltjes integration andtosolveitsrelatedproblems.
- **CO3** Work effectively in integration under integral sign.
- **CO4** Provide a strong foundation in the study of the convergence of infinite series, infinite product and uniform convergence and its interplay between various limiting operations.
- **CO5** Know about the convergence of sequences of functions.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No



Unit – 1 FunctionsofBoundedVariation

Introduction-Propertiesofmonotonicfunctions-Functionsofboundedvariation–Totalvariation-Additivepropertyoftotalvariation-Totalvariationon[a,x]asafunctionofx-Functionsofboundedvariationexpressedasthedifferenceoftwoincreasingfunctions-Continuousfunctions of bounded variation.

Chapter6 : Sections 6.1to 6.8

Unit – 2 TheRiemann-StieltjesIntegral

Introduction-Notation-ThedefinitionoftheRiemann-Stieltjesintegral–LinearProperties-Integrationbyparts-ChangeofvariableinaRiemann-Stieltjesintegral-ReductiontoaRiemannIntegral-Euler'ssummationformula-Monotonicallyincreasingintegrators,Upperandlowerintegrals-Additiveandlinearitypropertiesofupperandlowerintegrals -Riemann's condition-Comparison Theorems

Chapter 7 : Sections 7.1 to7.14

Unit - 3TheRiemann-StieltjesIntegral(Contd.)18 hours

Integrators of bounded variation-Sufficient conditions for the existence of Riemann Stielt jes integrals-Necessary conditions for the existence of Riemann-Necessary conditions for the existence

Stielt jes integrals Mean value theorems for Riemann-Stielt jes integrals-

The integrals as a function of the interval-Second fundamental theorem of integral calculus-

ChangeofvariableinaRiemannintegral-SecondMeanValueTheoremforRiemannintegral-Riemann-Stieltjesintegralsdependingonaparameter-Differentiation under theintegral sign.

Chapter7:Sections 7.15 to7.24

Unit – 4 InfiniteSeriesandInfiniteProducts

Absoluteandconditionalconvergence-Dirichlet'stestandAbel'stest–Rearrangementofseries-Riemann'stheoremonconditionallyconvergentseries.Doublesequences-Doubleseries-Rearrangementtheoremfordoubleseries-Asufficientconditionforequalityofiteratedseries Multiplicationofseries-Cesarosummability–Infinite products. **Chapter8:** Sections 8.8,8.15, 8.17, 8.18, 8.20,8.21 to 8.26

5

18 hours

18 hours

18 hours

Unit – 5 Sequence of Functions

Pointwise convergence of sequences of functions - Examples of sequences of real - valuedfunctions - Definition of uniform convergence - Uniform convergence and continuity - TheCauchy condition for uniform convergence - Uniform convergence of infinite series offunctions - Uniform convergence and Riemann - Stieltjes integration - Uniform convergenceanddifferentiation-Sufficientconditionforuniformconvergenceofaseries-Meanconvergence.**Chapter9**: Sections9.1 to 9.6, 9.8, 9.10, 9.11, 9.13

Text Book:

TomM.Apostol:MathematicalAnalysis,2ndEdition,Addison-WesleyPublishingCompanyInc. NewYork,(1997).

ReferenceBooks:

- 1. R.G. Bartle, Real Analysis, (1976), John Wileyandsons Inc.
- 2. W.Rudin, Principle of Mathematical Analysis (1976), McGraw Hill Company, New York.
- 3. S.C.MalikandSavitaArora,MathematicalAnalysis(1991),WileyEasternLimited,NewDel hi.
- 4. SanjayAroraandBansiLal,IntroductiontoRealAnalysis(1991),SatyaPrakashan,NewDelh i.
- 5. A.L.GuptaandN.R.Gupta, PrincipleofRealAnalysis (2003), PearsonEducation.

E-Materials

https://mathworld.wolfram.com/ https://onlinecourses.nptel.ac.in/noc21_ma63/preview https://ocw.mit.edu/courses/mathematics/18-100a-introduction-to-analysis-fall-2012/

Mapping with Programme Outcomes

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	Μ	S	S	S	Μ
CO2	S	S	Μ	Μ	S	Μ	S	S	S	Μ
CO3	S	S	М	Μ	S	Μ	S	S	S	Μ
CO4	S	S	Μ	Μ	S	Μ	S	S	S	М
CO5	S	S	Μ	Μ	S	Μ	S	S	S	Μ

* PO – Programme Outcome, CO – Course Outcomes

* S – Strong, M – Medium, L – Low

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

18 hours

6

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : I	Paper type : Core	Credit	:	4
Paper code :	Name of the Paper : Ordinary Differential Eq	uations		
Hours of Teaching:90 hrs				

Course Objectives:

The main objectives of this course are to:

- 1. Understand the theory and methods of Ordinary Differential Equations (ODEs).
- 2. Apply and solve ODEs applications from various emerging technologies.
- 3. Know about the concepts and solving methods of Second and nthorder linear differential equations.
- 4. Study the concepts and solving methods of differential equations with variable coefficients and regular singular point.
- 5. Examine the existence and uniqueness of solutions of differential equations.

Course Outcomes:

After successful completion of the course the student will be able to

- **CO1** Analyze the methods of second order homogeneous and non-homogeneous equations.
- CO2 Apply and solve the higher order homogeneous and non-homogeneous equations.
- **CO3** Define the methods to solve linear equations with variable coefficients.
- CO4 Discuss the linear equations with regular singular points.
- **CO5** Construct the solutions for first order equations.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	Yes
4	Yes	Yes	Yes	No	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1 Linear Equations with Constant Coefficients

18 hours

Second order homogeneous equations - Initial value problems for second order - Linear dependence and independence - A formula for the Wronskian - The non - homogeneous equation of order two.

Chapter 2:Sections 1 to 6

Unit - 2Linear Equations with Constant Coefficients (Continuation)18 hoursHomogeneous equations of order n - Initial value problems for order n - equations with realconstants - Non-homogeneous equations of order n - Annihilator method - Algebra of constantcoefficient operators.

Chapter 2:Sections 7 to 12

Unit - 3Linear Equations with Variable Coefficients18 hours

Initial value problems - Existence and Uniqueness theorems - Solutions to solve a nonhomogeneous equation – The Wronskian and linear independence - Reduction of the order of homogeneous equations - Homogeneous equation with analytic coefficients – The Legendre-Equation.

Chapter 3: Sections 1 to 8

Unit – 4Linear Equations with Regular Singular Points18 hours

Euler equation - Second order equations with regular singular points - general and exceptional cases - Bessel equation.

Chapter 4: Sections 1 to 4 and 6 to 8

Unit – 5 Existence and Uniqueness of Solutions to First Order Equations 18 hours

Equation with variables separated - Exact equations - The method of successive approximations - The Lipschitz condition - Convergence of the successive approximations.

Chapter 5: Sections 1 to 6

Text Book:

Earl A. Coddington, An introduction to ordinary differential equations (Indian Reprint), Prentice- Hall of India Ltd., New Delhi, 2009.



Reference Books:

- 1. Williams E. Boyce and Richard C. DI Prima, Elementary differential equations and boundary value problems, John Wiley and sons, New York, 1967.
- 2. George F Simmons, Differential equations with applications and historical notes, Tata McGraw Hill, New Delhi, 1974.
- 3. W.T.Reid, Ordinary differential equations, John Wiley and sons, New York, 1971.
- 4. M.D.Raisinghania, Advanced differential equations, S.Chand & Company Ltd., New Delhi, 2001.
- N.N. Lebedev, Special functions and their applications, Prentice Hall of India, New Delhi, 1965.

E-Materials:

- 1. https://nptel.ac.in/courses/111104031
- 2. https://nptel.ac.in/courses/122107037
- 3. <u>https://ocw.mit.edu/courses/mathematics/18-03-differential-equations-spring-2010/</u>
- 4. <u>https://nptel.ac.in/courses/111108081/</u>
- 5. <u>https://ocw.mit.edu/courses/mathematics/18-034-honors-differential-equations-spring-</u> 2009/syllabus/

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	S	М	S	S	М	L
CO2	S	S	М	L	S	М	S	S	М	М
CO3	S	S	М	S	М	S	М	М	М	S
CO4	S	S	М	М	М	S	М	М	М	S
CO5	S	S	М	L	S	S	S	S	М	М

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

Semester : I	Paper type : Core Elective	Credit	:	3
Paper code :	Name of the Paper : Probability Theory			
Hours of Teaching:90 hrs				

Course Objectives:

The main objectives of this course are to:

- 1. Study basic notions of experiments, events, probability, random variables and probability distributions.
- 2. Acquire knowledge on variousparameters and measures of the probability distributions.
- 3. Educatethecharacteristic functions and its properties.
- 4. Inculcate thespecial types of discrete and continuous probability distributions.
- 5. Learnthestrongtheoreticalbackgroundaboutthelimittheoremsanditsconsequences

Course Outcomes:

After successful completion of the course the student will be able to

- **CO1** Analyze the basics of probability and random variables.
- **CO2** Understand to handle parameters of the distribution.
- **CO3** Define the properties and functionalities of characteristic functions.
- CO4 Discuss the various special probability distributions.
- **CO5** Construct the solutions for real time applications using limits theorem.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	Yes
2	Yes	Yes	Yes	No	Yes	No
3	No	Yes	Yes	Yes	Yes	No
4	No	Yes	Yes	Yes	Yes	No
5	No	Yes	Yes	Yes	Yes	Yes

Unit – 1 ProbabilityandRandomVariables

RandomExperiments–SampleSpace–RandomEvents–ProbabilityAxioms–Conditional Probability – Mutual Exclusive Events – Independent Events – Addition andProduct Theorems on Probability – Theorem of Total Probability – Baye's Theorem –Random Variables – Probability Mass and Density Functions – Distribution Function – JointDistribution– MarginalDistribution– Conditional Distribution– Independent RandomVariables – Functions of Random Variables. **Chapter 1 :** Sections 1.1 to 1.7

Chapter 2:Sections2.1 to 2.9

Unit – 2 Parameters of theDistribution

Mathematical Expectation – Moments – The Chebyshev Inequality – Absolute Moments –Order Parameters – Moments of Random Vectors – Regression of the First and SecondTypes. **Chapter3 :** Sections3.1 to 3.8

Unit – 3 CharacteristicFunctions

Properties of Characteristic Functions – Characteristic Functions and Moments – Semi-Invariants – Characteristic Function of the Sum of the Independent Random Variables – DeterminationofDistributionFunctionbytheCharacteristicFunction–

CharacteristicFunctionofMultidimensionalRandomVectors–ProbabilityGeneratingFunctions. Chapter4 : Sections4.1 to 4.7

Unit – 4 SpecialProbabilityDistributions

Discrete Probability Distributions: One Point – Two Point – Bernoulli Trails – Binomial – Poisson – Polya – Hypergeometric Distributions – Continuous Probability Distributions:Uniform– Normal – Gamma – Beta– Cauchy–LaplaceDistributions. **Chapter5 :** Sections5.1 to 5.10

Unit – 5 LimitTheorems

StochasticConvergence-BernoulliLawofLargeNumbers-

ConvergenceofSequenceofDistributionFunctions –Levy-CramerTheorems– ThedeMoivre-Laplace Theorem –

The Lindeberg-Levy Theorem – LapunovTheroem.

11

18 hours

18 hours

18 hours

18 hours

18 hours

Text Book:

M.Fisz,*ProbabilityTheoryandMathematicalStatistics*,3rdEdition,JohnWileyandSonsInc., New York, 1963.

ReferenceBooks:

- 1. R.B.Ash, Real Analysis and Probability, Academic Press, New York, 1972.
- 2. K.L.Chung, *ACourseinProbability*, 2nd Edition, AcademicPress, New York, 1974.
- 3. R.Durrett, *Probability: TheoryandExamples*, 5thEdition, CambridgeUniversityPress, New York, 2019.
- 4. V.K.RohatgiandA.K.Md.EhsanesSaleh, *AnIntroductiontoProbabilityTheoryandMathematic alStatistics*, 2nd Edition, WileyEasternLtd., NewDelhi, 1988.
- B.R.Bhat, ModernProbabilityTheory– AnIntroductoryTextbook,4thEdition,NewAgeInternational Pvt.Ltd., New Delhi,2014.

E-Materials:

- 1. https://ocw.mit.edu/resources/res-6-012-introduction-to-probability-spring-2018/
- 2. https://www.coursera.org/learn/introductiontoprobability
- 3. <u>https://swayam.gov.in/nd1_noc20_ma18/preview</u>
- 4. <u>https://onlinecourses.nptel.ac.in/noc21_ma24/preview</u>

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
C01	S	S	S	М	М	S	М	М	М	М
CO2	S	S	S	S	М	S	М	М	S	М
CO3	S	S	S	S	М	М	М	S	М	М
CO4	S	S	М	М	S	М	М	S	S	S
CO5	S	S	М	S	М	М	М	S	S	S

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course OutcomesL

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Credit : 3

Semester : I	Paper type : Core Elective
Paper code :	Name of the Paper : Mechanics
Hours of Teaching:90 hrs	

CourseObjectives:

The main objectives of this courseare to:

- 1. Understand mechanical systems under generalized coordinate systems.
- 2. Apply mechanics techniques in virtual work.
- 3. Develop the students ability to deal with Energyandmomentum.
- 4. Look at the conceptof Hamilton, Lagrange.
- 5. Discuss the CanonicalTransformation.

CourseOutcomes

Afterthesuccessful completion of this course the students will be able to:

- **CO1** Explain the basics concepts of mechanical systems undergeneralized coordinate systems.
- CO2 Identify the Lagrange's equations and its application.
- **CO3** Derive the Hamilton Equation.
- **CO4** Analyze the Hamilton'sPrinciple and Hamilton-JacobiEquationandseparability.
- **CO5** Discuss the LagrangeandPoissonbrackets.

Unit	Remembering	Understanding	Understanding Applying Anal		Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	Yes
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	Yes

Unit – 1 MechanicalSystems

TheMechanicalsystem-Generalizedcoordinates- Constraints-Virtualwork–EnergyandMomentum. **Chapter1:** Sections 1.1 to 1.5

18 hours

Unit - 2Lagrange's Equations18 hoursDerivation of Lagrange's equations- Examples - Integrals of motion.18 hoursChapter 2: Sections2.1 to 2.3

Unit - 3Hamilton's Equations18 hoursHamilton's Principle - Hamilton's Equation - Other variational principle.18 hoursChapter4: Sections 4.1 to 4.3

Unit – 4Hamilton-JacobiTheory18 hoursHamilton Principal function - Hamilton-Jacobi Equation – Separability.18 hours

Chapter5: Sections 5.1 to 5.3

Unit - 5CanonicalTransformation18 hoursDifferential forms and generating functions - Lagrange and Poisson brackets.

Differential forms and generating functions - Lagrange a

Chapter 6:Sections6.1 and 6.3

Text Book:

D.T.Greenwood, *ClassicalDynamics*, PrenticeHallof India, NewDelhi, 1985.

ReferenceBooks:

- 1. H.Goldstein, *ClassicalMechanics*, (2ndEdition) NarosaPublishingHouse, NewDelhi.
- 2. N.C.RaneandP.S.C.Joag, *ClassicalMechanics*, TataMcGrawHill, 1991.
- J.L.Synge and B.A.Griffth, *Principles of Mechanics* (3rd Edition) McGraw HillBookCo., New York, 1970.

E-Materials:

https://ocw.mit.edu/courses/physics/8-09-classical-mechanics-iii-fall-2014/

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Cos	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	Μ	S	Μ	L	Μ	S	L	S	L
CO2	Μ	S	Μ	S	S	L	Μ	S	L	Μ
CO3	S	S	Μ	S	Μ	L	S	S	Μ	L
CO4	Μ	L	Μ	L	S	Μ	Μ	L	L	S
CO5	S	S	Μ	S	L	Μ	Μ	S	L	S

Mapping with Programme Outcomes

* PO – Programme Outcome, CO – Course Outcomes

Semester : I	Paper type : Core Elective	Credit	:	3
Paper code :	Name of the Paper : Graph theory			
Hours of Teaching: 90 hrs				

Course Objectives:

The main objective of this course are to:

- 1. Formally study and develop the basic concepts of Graphs.
- 2. Familiar with the notion and properties of varied types of graphs.
- 3. Understand concepts that helps to model real life situations into graphs.
- 4. Formulate and prove central theorems about trees, matching, connectivity, coloring and planarity of graphs.
- 5. Learn the proving techniques that are existing in each and every section of the unit and, motivate to do research in various fields of Graph theory.

CourseOutcomes

Afterthesuccessful completion of this course the students will be able to:

- **CO1** Grasp features and properties of various types of graphs.
- **CO2** Demonstrate capacity of illustration for mathematical reasoning through analyzing, providing and explaining concepts of Eulerian circuits and Hamiltonicity in graphs.
- CO3 Understand the definitions and properties of matching and independent sets.
- CO4 Apply the concepts of graphs to model them in real life situations.
- **CO5** Explicate the applications of planarity and colorability.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	Yes

Unit – 1 Graphs, Subgraphs And Trees

Graphs - Graph Isomorphism - The Incidence and Adjacency Matrices - Subgraphs - Vertex Degrees - Paths and Connection - Cycles - Trees - Cut Edges and Bonds - Cut Vertices- Cayley's formula- Application: The shortest path problem.

Chapter 1: Sections 1.1 to 1.8

Chapter 2: Sections 2.1 to 2.4

Unit – 2 Connectivity, Euler Tours and Hamilton Cycles

Connectivity - Blocks - Euler tours - Hamilton Cycles. Application: The travelling Salesman Problem.

Chapter 3: Sections 3.1 to 3.3

Chapter 4: Sections 4.1 to 4.2

Unit – 3 Matchings, Edge Colourings

Matchings - Matchings and Coverings in Bipartite Graphs –Perfect matchings- Edge Colourings:
Edge Chromatic Number - Vizing's Theorem. Application: Optimal Assignment Problem.
Chapter 5: Sections 5.1 to 5.3, 5.5
Chapter 6:Sections 6.1 to 6.2

Unit - 4Independent Sets And Cliques, Vertex Colourings18 hoursIndependent sets - Ramsey's Theorem - Vertex Colourings: Chromatic Number - Brooks'Theorem - Hajos Conjecture- Chromoatic polynomial.Chapter 7: Sections 7.1 to 7.2

Chapter 8: Sections 8.1 to 8.2, 8.4

Unit – 5 Planar Graphs

Plane and planar Graphs - Dual graphs - Euler's Formula - The Five-Colour Theorem and the Four-Colour Conjecture- Directed graphs.

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Chapter 9: Sections 9.1 to 9.6 and 10.1

18 hours

18 hours

18 hours

18 hours

Text Book:

J.A.Bondy and U.S.R. Murthy, Graph Theory and Applications, Macmillan, London, 1976.

Reference books:

- Narsingh Deo, Graph Theory with applications to engineering and computerscience, Prentice Hall of India, New Delhi,2001
- G.Chartrand and L.Lesniak, Graphs and Digraphs, Chapman and Hall, CRC, Fourth Edition, 2005
- 3. R.J. Wilson, *Introduction to Graph Theory*, Pearson Education, 4th Edition, 2004,Indian Print.
- 4. S. A. Choudum, *A First Course in Graph Theory*, MacMillan India Ltd. 1987.
- 5. J. Clark and D.A. Holton, A First look at Graph Theory, Allied Publishers, NewDelhi, 1995.
- 6. A. Gibbons, *Algorithmic Graph Theory*, Cambridge University Press, Cambridge, 1989.

E- Materials:

https://nptel.ac.in/courses/111106050/

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	Μ	S	S	S	S	S
CO2	S	S	Μ	Μ	S	S	S	S	S	S
CO3	S	S	Μ	Μ	S	S	S	S	S	S
CO4	S	S	S	S	S	S	S	S	S	S
CO5	S	S	S	S	S	S	S	S	S	S

Mapping with Programme Outcomes

* PO – Programme Outcome, CO – Course Outcomes

Semester : IPaper type:OpenElectiveCredit : 3Paper code :Name of the Paper : BasicMathematicsHours of Teaching: 90 hrs

CourseObjectives:

The main objective of this course are to:

- 1. Studyexponentialandlogarithmicseries.
- 2. Understandaboutmatricesanditsapplications.
- 3. Formulateandsolvethepartialdifferentialequations.
- 4. Discuss the properties of Laplace and inverse Laplace transformation.
- 5. Learnthe expansiontechniquesofFourierseries.

CourseOutcomes:

Aftersuccessful completion of the course the student will be able to

- **CO1** Evaluate the exponential and logarithmic series.
- CO2 Explainaboutmatrices and its applications.
- CO3 Solvethepartial differential equations.
- CO4 Solvethedifferentialequations using Laplacetransform.
- CO5 Analysethetechniques of Fourierseries.

Unit	Remembering	g Understanding Applying Analyzing		Evaluating	Creating	
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	No	No	Yes	No
3	Yes	Yes	Yes	No	Yes	No
4	Yes	Yes	No	No	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1 ExponentialandLogarithmicseries

Exponentialseries-Logarithmicseries

Chapter 1:Section1.1–1.2

Unit – 2 Matrices

Determinantofamatrix–Characteristicequationofamatrix–Characteristicvectorsofamatrix–Cayley-HamiltonTheorem–Inverseof amatrix.

Chapter4:Section4.1–4.5

Unit – 3 PartialDifferentialEquations

Elimination of arbitrary constants – Elimination of arbitrary functions – Standard forms – Lagrange'sEquations.

Chapter9: Section 9.1 – 9.4

Unit – 4 Laplacetransforms

Properties of Laplace transform-Inverse Laplace transform-Partial Fractions.

Chapter10:Section 10.1 – 10.3

Unit – 5 FourierSeries

Properties of Integration – Odd and Even Functions – Half Range Fourier Series. **Chapter11:** Section11.1 – 11.3

Text Book:

G.BrittoAntonyXavier,V.Balaji,S.U.VasanthaKumar,B.Govindan,MathematicalSciences, JayalakshmiPublications, 2-e,2015.

ReferenceBooks:

- 1. P. Balasubramaniyam,K.G. Subramanian,AncillaryMathematics,Volume– I,TataMcGrawHill publishingcompanylimited, NewDelhi,1996.
- 2. P.DuraiPandian,S.UdayaBaskaran,AlliedMathematics,Volume–I,Muhilpublishers,1st Edition, Chennai, 1997.
- 3. P.KandsamyandK.Thilagavathy,AlliedMathematicsvolume–I,Volume–I,S.Chand&Company, New Delhi, 2004.
- 4. ShantiNarayan, P.K. Mittal, Differential Calculus, S. Chand & Co, New Delhi, 2005.
- 5. A.Singaravelu, Allied Mathematics, Meenakshi Agency, Chennai, 2001.
- 6. P.R.Vittal, Allied Mathematics, Margham Publications, Chennai, 1999.

20

18 hours

18 hours

18 hours

18 hours

18 hours

E-Materials:

http://mathforum.org/library/drmath/sets/elem_2d

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	S	S	S	L	S
CO2	S	S	Μ	Μ	S	S	S	S	L	S
CO3	S	S	Μ	Μ	S	S	S	S	Μ	S
CO4	S	S	Μ	Μ	S	S	S	S	Μ	S
CO5	S	S	Μ	Μ	S	S	S	S	Μ	S

Mapping with Programme Outcomes

* PO – Programme Outcome, CO – Course Outcomes

Semester : I	Paper type : Open Elective	Credit	:	3
Paper code :	Name of the Paper : Mathematical Foundation	S		
Hours of Teaching: 90 hrs				

CourseObjectives:

The main objective of this course are to

- 1. Study the logical operators , Propositional function, quantifiers, rules of inference.
- 2. Understand about fundamental mathematical concepts such as sets, relations, functions and composition functions
- 3. Know the types of binary operations and boolean algebra.
- 4. Formulateandsolve he differentiation and applications of differentiation
- 5. Acquire the knowledge of two dimensional analytical geometry

CourseOutcomes:

Aftersuccessful completion of the course the student will be able to

- CO1 Applymathematicallogicaloperators.
- CO2 Improveknowledgeinset theory, functions with some problems.
- CO3 Classify the types of binary operations and know about the boolean algebra.
- CO4 Solveproblemsonapplicationsofdifferentiation
- **CO5** Evaluate problems on Straight lines, circles and conics.

Unit	Remembering	Understanding	nding Applying Analyzing		Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	No
2	Yes	Yes	No	No	Yes	Yes
3	Yes	Yes	No	Yes	Yes	No
4	Yes	Yes	No	No	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1 **SymbolicLogic**

Proposition, Logical operators, conjunction, disjunction, negation, conditional and Biconditionaloperators, converse, inverse, contrapositive, logically equivalent, tautology and contradiction, Arguments and validity of argument.

Chapter1:Sections 1.1–1.5

Unit -2SetTheory

Set, Setoperations, Venndiagram, Properties of sets, number of elements in a set, Cartesian product, relation & functions, Relation: Equivalencerelation. Equivalence class, Partially and Totally ordered sets, Functions :Types ofFunctions,CompositionofFunctions.

Chapter2:Sections 2.1–2.8

Unit -3**Binary Operations**

TypesofBinaryoperations:Commutative,Associative,Distributiveandidentity,Booleanalgebra:properti es,Permutationsandcombinations.

Chapter3:Sections 3.1–3.3

Unit – 4 Differentiation 18 hours Simple problem using standard limits, $\lim_{x \to a} \frac{x^n - a^n}{x - a}$, $\lim_{x \to 0} \frac{\sin x}{x}$, $\lim_{x \to 0} \frac{\tan x}{x}$, $\lim_{x \to 0} e^x$, $\lim_{n \to 0} \frac{(1 + 1/n)^n}{n}$, $\lim_{n \to \infty} (1+n)^{1/n}$, Differentiation,

successivedifferentiation,Leibnitztheorem,partialDifferentiation,Applications of differentiation, Tangent and normal, angle between two curves, Maximum and minimum values [second derivative test], curvature and radius of curvature [Cartesian coordinates], Envelopes. Chapter 4: Sections 4.1 - 4.9

Unit – 5 **TwoDimensionalAnalyticalGeometry**

Straight lines – pair of straight lines – circles – System of Circles – Conics [parabola, Ellipseand Hyperbola].

Chapter 5: Sections 5.1 - 5.5

Text Book:

U.Rizwan, Mathematical Foundations Volume I, Nelliappar Publications, Chennai 2017.

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18 hours

18 hours

18 hours

18 hours

ReferenceBooks:

- 1. P.R.Vittal, Mathematical Foundations, Margham Publication, Chennai.
- 2. V.Sundaram &others,DiscreteMathematicalFoundations,A.P.Publication,Sirkali
- P.Duraipandian&Others,AnalyticalGeometryof2and3Dimensions,EmeraldPublication 1992 Reprint.

E-Materials:

http://www.mathfoundation.com

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	М	L	S	S	Μ	S
CO2	S	S	Μ	Μ	S	Μ	S	Μ	Μ	S
CO3	S	S	Μ	Μ	S	S	S	S	Μ	S
CO4	S	S	S	L	S	S	S	S	Μ	S
CO5	S	S	S	S	М	S	S	S	М	S

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : I

Paper code :

Paper type : OpenElective

Credit : 3

Name of the Paper : MathematicalModeling

Hours of Teaching:90 hrs

Course objective:

The main objective of this course are to

- 1. Provide an introduction to modeling and simulation.
- 2. Solve and interpret real life problems using different Mathematical perspectives.
- 3. Apply the Mathematical Modeling through difference equations.
- 4. Develop the Mathematical modeling through Graphs.
- 5. To have a proper understanding of calculus of variations and Dynamics Programming.

Course Learning outcomes:

After the successful completion of this course, the students will be able to:

- **CO1** Understand concept of modeling and simulation.
- **CO2** Crete mathematical models of real world problems.
- **CO3** Explain the population dynamics and genetics.
- CO4 Mathematical models using mathematical techniques.
- **CO5** Discuss the calculus Variations and Dynamic Programming.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	No	Yes	No
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	Yes

Unit – 1 Mathematical Modelling through Systems of Ordinary 18 hours differential Equations of the First Order

Mathematicalmodellinginpopulationdynamics, Mathematicalmodelling ofepidemicsthrough systems of ordinary differential equations of first order - Mathematical Models inMedicine, Arms Race, Battles and international Trade in terms of Systemsof ordinary differential equations - Mathematical modelling in dynamics through systems of ordinarydifferential equations of first order.

Chapter 3:Sections 3.1, 3.2, 3.5 and 3.6

Unit -2Mathematical Modellingthroughdifference equations 18 hours

The need for Mathematical modelling through difference equations - some simple models -Basictheoryoflineardifferenceequationswithconstantcoefficients-Mathematicalmodellingthrough difference equations in economicsandfinance.

Chapter5:Sections 5.1to 5.3

Unit – 3 Mathematical Modellingthroughdifferenceequations(contd.) 18 hours

Mathematical modelling through difference equations in population dynamics and genetics.Mathematical Modelling through difference equations in probability theory. Miscellaneousexamples of Mathematical modelling through difference equations.

Chapter 5:Sections 5.4 to 5.6

Unit – 4 Mathematical modellingthroughGraphs

Situations that can be modeled through graphs - Mathematical models in terms of directed graphs - Mathematical models in terms of signed graphs - Mathematical models in terms ofweightedgraphs.

Chapter7:Sections 7.1 to 7.4

Unit – 5 MathematicalModellingthroughcalculusofVariationsand 18 hours **DynamicProgramming**

Optimization principles and techniques-Mathematical modelling through calculus of variations-

MathematicalModellingthroughdynamicprogramming.

Chapter9:Sections 9.1to9.3

Text Book:

J.N.Kapur, Mathematical Modelling, Willey Eastern Limited, Reprint, 2000.

26

18 hours

ReferenceBooks:

- 1. D.J.G.JamesandJ.J.Macdonald,CasestudiesinMathematicalModelling,StanlyThames,C heltonham.
- 2. M.CrossandA.O.Moscrcadini,TheartofMathematicalModelling,EllisHarwoodandJohn Wiley.
- 3. C.Dyson, Elvery, Principles of Mathematical Modelling, Academic Press, New York.
- 4. D.N.Burghes, Modelling with Difference Equations, Ellis Harwood and John Wiley.

E-Materials:

http://www.mathfoundation.com

Mapping with Programme Outcomes

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	Μ	S	Μ	S	Μ	S	L	S	L
CO2	Μ	S	Μ	S	Μ	L	Μ	L	L	S
CO3	S	L	S	Μ	S	L	Μ	S	L	М
CO4	Μ	S	Μ	S	S	Μ	L	S	Μ	S
CO5	S	L	Μ	S	Μ	Μ	L	Μ	L	S

* PO – Programme Outcome, CO – Course Outcomes

Semester : II	Paper type : Core	Credit : 5
Paper code :	Name of the Paper : Algebra-II	
Hours of Teaching:90 hrs		

Course Objective:

The main objective of this course are to :

- 1. Attain depth knowledge about extension field and its types.
- 2. Study the concepts of existence of extension fields of polynomials over polynomial rings.
- 3. Understand Galois theory and develop Galois groups.
- 4. Know more about the finite fields and solvable groups.
- 5. Learn the important theorems related to division rings and its application.

Course Learning Outcomes:

After successful completion on the course the student will be able to:

- **CO1** Understand fundamental concepts including extension fields, Algebraic extensions and Algebraic numbers.
- CO2 Determine existence and properties of extension fields of polynomials
- **CO3** Demonstrate capacity of illustration for mathematical reasoning through analyzing, proving and explaining concepts from filed extensions and Galois theory
- CO4 Apply knowledge of solvability of radicals over polynomials on finite fields
- CO5 Analyze the theorems related to division rings to apply them on relevant fields

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	No	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1 Field Theory	18 hours
Extension fields - Transcendence of 'e'.	
Chapter 5: Section 5.1 and 5.2	
Unit – 2 Polynomials and Roots	18 hours
Roots of Polynomials- More about roots.	
Chapter 5: Sections 5.3 and 5.5	
Unit – 3 Galois theory	18 hours
Elements of Galois theory.	
Chapter 5: Section 5.6	
Unit – 4 Finite Fields	18 hours
Solvability by Radicals - Finite fields - Wedderburn's theorem on finite division rings.	
Chapter 5: Section 5.7	
Chapter 7: Sections 7.1 and 7.2 (Only Theorem 7.2.1)	

Unit - 5Solvability by Radicals18 hoursA theorem of Frobenius - Integral Quaternions and the Four -Square theorem.18 hours

Chapter 7 : Sections 7.3 and 7.4

Text Book:

I.N. Herstein, Topics in Algebra, 2nd Edition. Wiley.1975

Reference Books:

- 1. D.S.Dummit and R.M.Foote. Abstract Algebra. Wiley 2003.
- 2. M. Artin, Algebra, Prentice Hall of India, 1991.
- 3. J.A. Gallian. Contemporary Abstract Algebra. 4th Edition. Narosa Publishing 2011.
- 4. P.B.Battacharya, S.K.Jain and S.R.Nagpaul, Basic Abstract Algebra(II Edition) Cambridge University Press, 1997.(Indian Edition)
- 5. I.S. Luther and I.B.S.Passi, Algebra, Vol.I Groups(1996), Vol. II Rings, Narosa Publishing House, New Delhi, 1999.
- 6. Rudolf Lidl and Gunter Pilz, Applied Abstract Algebra, Second Indian Reprint 2006, Springer Verlag, Newyork.
- L. Smith(1998). Linear transformation: Example and Applications. In: Linear Algebra, Undergraduate texts in Mathematics, Springer, Newyork.

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E-Materials:

- 1. https://www.jmilne.org->FTe6
- 2. http://www.math.iitb.ac.in/~srg/Lecnotes/galois_des.html
- 3. <u>https://www.jmilne.org>math</u>
- 4. <u>https://nptel.ac.in/courses/111108098/</u> (Video Lecture)

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	Μ	Μ	S	S	S	S
CO2	S	S	Μ	Μ	Μ	S	S	S	S	S
CO3	S	S	Μ	Μ	Μ	Μ	S	S	S	S
CO4	S	S	Μ	Μ	Μ	S	S	S	S	S
CO5	S	S	Μ	Μ	Μ	Μ	S	S	S	S

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

Semester : II

Paper code :

Paper type : Core Name of the Paper : Real Analysis-II Credit : 5

Hours of Teaching:90 hrs

CourseObjectives:

Theobjectives of the courseis to

- 1. know the Lebesgue Integral
- 2. understand the concept of Riesz-Fischer theorem
- 3. studyFourierSeriesand Integralsindepth
- 4. understandtheconcepts of multivariable calculus.
- 5. acquire knowledgeabout implicit functions and the extremum values of functions.

Course Outcomes:

After successful completion on the course the student will be able to

- **CO1** know about the properties of Lebesgue integrals and establish the Levi monotone convergence theorem.
- **CO2** develop the properties of inner products, norms and measurable functions.
- CO3 understand the concept of FourierSeries and Integrals.
- CO4 acquire the knowledge of multivariable calculus.
- **CO5** enrich the students to work effectively on implicit functions and the extremum valuesof functions.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	No	Yes	No

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Unit – 1 Lebesgue Integral

Introduction- The integral of a step function – Monotonic sequences of step functions – Upper functions and their integrals - Riemann-Integrable functions as examples of upper functions -The class of Lebesgue- Integrable functions on a general interval - Basic properties of the Lebesgue integral - Lebesgue integration and sets of measure zero - The Levi monotone convergence theorems-Lebesgue Dominated Convergence Theorem.

Chapter 10: Sections 10.1 to 10.10

Unit -2Lebesgue Integral Contd.

Lebesgue integrals on unbounded intervals as limits of integrals on bounded intervals –Improper Riemann integrals - Measurable functions - Continuity of functions defined byLebesgue integrals – Differentiation under the integral sign – Inner products and norms – The set L^2 (I) of square-integrable functions – The set L^2 (I) as a semi-metric space – A convergence theorem for series of functions in $L^{2}(I)$ – The Riesz-Fischer theorem.

Chapter 10: Sections 10.12 to 10.16, 10.21 to 10.25

Unit – 3 **FourierSeries andFourierIntegrals**

Introduction-Orthogonalsystemoffunctions-Thetheoremonbestapproximation-TheFourierseriesoffunctionrelativetoanorthonormalsystem-PropertiesofFourierCoefficients-TheRiesz-FischerTheorem-Theconvergenceandrepresentationproblemsfortrigonometricseries-TheReimann-LebesgueLemma-TheDirichletIntegrals-AnIntegralrepresentationforthepartialsumsofFourierseries-Reimann'slocalizationtheorem-SufficientconditionsforconvergenceofaFourierSeriesataparticularpoint-CesarosummabilityofFourierseries-ConsequencesofFejes'stheorem-

TheWeiestrassapproximationtheorem.

Chapter11:Sections11.1 to 11.15

18 hours

18 hours

Unit – 4 MultivariableDifferentialCalculus

Introduction–TheDirectionalderivative–Directionalderivativeandcontinuity–Thetotalderivative– Thetotalderivativeexpressed interms of partial derivatives–AnApplications to Complex– Valued Functions-Thematrix of linear function–The Jacobian matrix–The chain rule– Matrix form of chain rule–Themean-value theorem for differentiable functions– Asufficient condition for differentiability–Asufficient condition for equality of mixed partial derivatives– Taylor's theorem for functions of Rⁿ to R¹.

Chapter12:Sections 12.1 to12.14

Unit – 5 ImplicitFunctionsandExtremumProblems 18 hours

Introduction-Functionswithnon-zeroJacobiandeterminants—Theinversefunctiontheorem— TheImplicitfunctionTheorem—Extremaofrealvaluedfunctionsofonevariableandseveralvariables— Extremumproblemswithsideconditions.

Chapter13:Sections13.1 to 13.7

Text Book:

TomM.Apostol,MathematicalAnalysis(SecondEdition)(1981),Addison–WesleyPublishingCompanyInc.New York.

ReferenceBooks:

- 1. J.C.Burkill, TheLebesgue Integral(1951), Cambridge UniversityPress.
- 2. M.E.Munroe, Measure And Integration (1971), Addison–Wiley.
- 3. H.L.Roydon, Real Analysis (1988), Macmillan Pub. Company, New York.
- 4. W.Rudin, Principles of Mathematical Analysis (1979), McGraw Hill Company, New York.
- 5. S.C.MalikandSavitaArora,MathematicalAnalysis(1991),WileyEasternLimited,NewDel hi.
- 6. SanjayArora andBansiLal,SatyaPrakashan,IntroductionTo RealAnalysis,(1991),NewDelhi.

E-Materials:

https://onlinecourses.nptel.ac.in/noc21_ma63/preview https://mathworld.wolfram.com/ https://ocw.mit.edu/courses/mathematics/18-100b-analysis-i-fall-2010/

to12.14

18 hours

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COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	Μ	S	S	S	Μ
CO2	S	S	Μ	Μ	S	Μ	S	S	S	Μ
CO3	S	S	Μ	Μ	S	Μ	S	S	S	Μ
CO4	S	S	Μ	Μ	S	Μ	S	S	S	М
CO5	S	S	Μ	Μ	S	Μ	S	S	S	Μ

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II	Paper type : Core	Credit	:	4
Paper code :	Name of the Paper : Partial Differential Equat	ions		
Hours of Teaching:90 hrs				

Course Objectives:

The main objective of this course are to:

- 1. Understand the theory and methods of Partial Differential Equations (PDEs).
- 2. Apply and solve PDEs applications from various emerging technologies.
- 3. Provide solution for First and second order partial differential equations.
- 4. Introduce the concepts and solving methods of Elliptical, paraboloid, hyperbolic differential equations.
- 5. Examine the existence and uniqueness of solutions of differential equations.

Course Outcomes:

After successful completion of the course the student will be able to

- **CO1** Analyze the methods for first order partial differential equations.
- CO2 Understand the fundamentals of second order partial differential equations.
- **CO3** Define the methods to solve elliptical differential equations.
- CO4 Discuss the formation and solutions of paraboloid differential equations.
- **CO5** Construct the solutions for hyperbolic differential equations and identifythe research problem where PDE can be used to model the problem.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	Yes

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Unit – 1 Partial Differential Equations of First Order

Formation and solutions of first order PDE – Integral surfaces – The Cauchy problem for first order equation –Orthogonal surfaces – First order non-linear equations – characteristics– compatible systems of first order equations - Charpit's method.

Chapter 0:Sections 0.4 to 0.11. (omit 0.11.1))

Unit – 2 Fundamentals of Second Order PDE

Introduction – classification of second order PDE – canonical forms – Adjoint operators. **Chapter 1:S**ections 1.1 to 1.4

Unit – 3 Elliptic Differential Equations

Derivation of Laplace and Poisson equations – Boundary value problem – Separation of variables – Dirichlet's and Newmann problems for a rectangle – Solution of Laplace equation in Cylindrical and spherical coordinates.

Chapter 2: Sections 2.1, 2.2, 2.5 to 2.7,2.11 to 2.12

Unit – 4 Parabolic Differential Equations

Formation and elementary solution of diffusion equation with boundary conditions – Dirac-Delta function – Separation of variable method - Solution of diffusion equation in cylindrical and spherical coordinates.

Chapter 3: Sections 3.1 to 3.7

Unit – 5 Hyperbolic Differential Equations

Derivation and solution of 1-D wave equation by canonical reduction – Initial Value Problem ; D'Alembert's solution – IVP and BVP for 2-D wave equation – Periodic solution for 1-D wave equation in cylindrical and spherical coordinates systems –Uniqueness of the solution for 1-D wave equation – Duhamel's principle.

Chapter 4: Sections 4.1 to 4.4, 4.7 to 4.9, 4.11 and 4.12

Text Book:

K.Sankara Rao, Introduction to Partial differential equations (Third edition), Prentice-Hall of India Ltd., New Delhi, 2016.

36

18 hours

.

18 hours

18 hours

Reference Books:

- I.N. Sneddon, Elements of partial differential equations, McGraw Hill book company, Singapore, 1957
- 2. R. Dennemeyer, Introduction to partial differential equations and boundary value problems, McGraw Hill, New York, 1968.
- 3. R.C. McOwen, Partial differential equations, 2nd edition, Pearson education, New Delhi, 2005.
- 4. M.D.Raisinghania, Advanced differential equations, S.Chand& Company Ltd. New Delhi, 2001.
- 5. N.N. Lebedev, Special functions and their applications, Prentice Hall of India, New Delhi, 1965.

E-Materials:

- 1. https://nptel.ac.in/courses/111103021/
- 2. onlinecourses.nptel.ac.in > noc21_ma18
- 3. onlinecourses.nptel.ac.in > noc22_ma28
- 4. onlinecourses.nptel.ac.in > noc21_ma33

Mapping with Programme Outcomes

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	М	S	М	S	М	М
CO2	S	S	М	М	М	S	М	S	М	S
CO3	S	S	S	М	М	S	S	М	М	S
CO4	S	S	S	М	М	М	S	М	М	S
CO5	S	S	S	М	М	М	S	М	М	S

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II

Paper code :

Paper type : Core Elective

Name of the Paper : Mathematical Statistics

Credit : 3

Hours of Teaching: 75 hrs

Course Objectives:

The main objective of this course are to:

- 1 Introduce the basic notions of sample, population, sample moments and their functions.
- 2 Give an insight about the parametric and non-parametric tests for small and large samples.
- 3 Educate the various measures of estimation theory
- 4 Inculcate the concepts of ANOVA and testing of hypothesis.
- 5 Indoctrinate the strong background about the sequential analysis and its consequences.

Course Outcomes:

After successful completion on the course the student will be able to

- **CO1** Know the basic notions of sample, population, sample moments and their functions.
- **CO2** Comprehend the parametric and non-parametric tests for small and large samples.
- **CO3** Understand the various measures of estimation theory.
- **CO4** Acquire the knowledge in the concept of ANOVA and, apply them in real life situations for testing of hypothesis.
- **CO5** Procure the strong background about the sequential analysis and its consequences

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	Yes	Yes	No
2	Yes	Yes	No	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

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Unit – 1 **Sample Moments and Their Functions**

Notion of a Sample and a Statistic - Distribution of the Arithmetic Mean of IndependentNormally Distributed Random Variables - The Chi-Square Distribution - The Distribution of the Statistics - Student's t-Distribution - Fisher's Z-Distribution - Snedecor's F Distribution-Distribution of Sample Mean from Non-Normal Populations.

Chapter 9: Sections: 9.1–9.8

Unit -2**Significance Tests**

Kolmogorov Theorem - Smirnov Theorem - The Concept of a Statistical Test - ParametricTests for Small Samples and Large Samples - Chi-Square Test - Tests of Kolmogorov and Smirnov Type – The Wald-Wolfovitz and Wilcoxon-Mann-Whitney Tests – Independence Tests by Contingency Tables.

Chapter 10:Sections: 10.11 Chapter 12: Sections: 12.1–12.7

Unit -3**Estimation Theory**

Preliminary Notion - Consistent Estimaties - Unbiased Estimates - Sufficiency of anEstimate -Efficiency of an Estimate - Asymptotically Most Efficient Estimates - Methodsof Finding Estimates-Confidence Interval.

Chapter 13: Sections: 13.1–13.8

Unit -4**Analysis of Variance and Hypotheses Testing** 15 hours

ANOVA Test: One-Way Classification and Two-Way Classification. Hypotheses Testing:The Power Functions and OC Function – Most Powerful Test – Uniformly Most PowerfulTest – Unbiased Test.

Chapter 15: Sections 15.1–15.2

Chapter 16:Sections 16.1–16.5

Unit – 5 **Elements of Sequential Analysis**

SPRT - Auxiliary Theorem - Wald's Fundamental Identity - OC Function and SPRT -The Expected Value of (n) – Determination of A and B – Testing a Hypothesis Concerning pof Zero-One Distribution – Testing a Hypothesis Concerning the Expected Value m of aNormal Population.

Chapter 17: Sections: 17.1–17.9

39

15 hours

15 hours

15 hours

Text Book:

M. Fisz, Probability Theory and Mathematical Statistics, 3rd Edition, John Wileyand Sons Inc., New York, 1963.

Reference Books:

- 1. V.K. Rohatgi and A.K.Md.E. Saleh, An Introduction to Probability Theory andMathematical Statistics, 2nd Edition, Wiley Eastern Ltd., New Delhi, 1988.
- E.J. Dudewicz and S.N. Mishra, Modern Mathematical Statistics, John Wiley and Sons, New York, 1988.
- 3. G.G. Roussas, A First Course in Mathematical Statistics, 2nd Edition, AcademicPress, USA, 1997.
- 4. B.L.V.D. Waerden, Mathematical Statistics, Springer-Verlag, New York, 1969.
- 5. R.E. Walpole, R.H. Myers, S.L. Mayers and K. Ye, Probability and Statistics forEngineers and Scientists, 9th Edition, Pearson Education Inc., 2012.

E-Materials:

- 1. https://ocw.mit.edu/courses/18-655-mathematical-statistics-spring-2016/
- 2. <u>https://dspace.mit.edu/bitstream/handle/1721.1/96865/18-175-fall-2008/contents/lecture-notes/index.htm</u>
- 3. https://swayam.gov.in/nd1_noc20_ma19/preview
- 4. http://mathworld.wolfram.com

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	S	S	S	S	S	S	S	S
CO2	S	S	S	S	S	S	S	S	S	S
CO3	S	S	S	S	Μ	S	S	S	S	S
CO4	S	S	S	S	S	S	S	S	S	S
CO5	S	S	S	S	М	S	S	S	S	S

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IIPaper type : Core ElectiveCredit : 3Paper code :Name of the Paper : Fuzzy Set Theory

Hours of Teaching: 75hrs

Course Objectives:

The main objective of this course are to

- 1. Introduce Fuzzy sets.
- 2. Define some operations on Fuzzy sets.
- 3. Understand the properties of Fuzzy sets.
- 4. Discuss about the operations on Fuzzy sets.
- 5. Calculate the arithmetic operations on Fuzzy numbers.

Course Outcomes:

After successful completion on the course the student will be able to

- CO1 Understand the basic concepts of Fuzzy Sets.
- CO2 Discuss the Fuzzy sets versus crisp sets.
- CO3 Analyze the operations on Fuzzy sets and Fuzzy complements.
- **CO4** Acquire the knowledge of various combination of operations.
- **CO5** Apply the concepts of Fuzzy mathematics in real life situation.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	No	No
2	Yes	Yes	No	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	No	Yes	Yes

Unit - 1From Classical (Crisp) Sets to Fuzzy Sets15 hoursIntroduction - Crisp sets: An overview - Fuzzy sets - Basic types - Basic concepts -Characteristics - Significance of the paradigm shift.Chapter 1: Sections 1.1 to 1.5

Unit - 2Fuzzy Sets Versus Crisp Sets15 hours

Additional properties of α - Cuts – Representation of Fuzzy sets – Extension principle for Fuzzy sets.

Chapter 2: Sections 2.1 to 2.3

Unit - 3Operations on Fuzzy Sets15 hoursTypes of Operation – Fuzzy complements – Fuzzy intersection – t-norms5 hoursChapter 3: Sections 3.1 to 3.35 hours

Unit - 4Operations on Fuzzy Sets15 hoursFuzzy unions - t conorms - Combinations of operations - Aggregation operations.15 hoursChapter 3: Sections 3.4 to 3.6

Unit - 5Fuzzy Arithmetic15 hoursFuzzy numbers - Linguistic Variables - Arithmetic operation on intervals - Arithmetic operationon Fuzzy numbers.

Chapter 4: Sections 4.1 to 4.4

Text book :

G. J. Klir and Bo Yuan, Fuzzy Sets and Fuzzy Logic : Theory and Applications, PHI, New Delhi, 2005.

Reference Books:

- 1. H. J. Zimmerman, Fuzzy Set Theory and its Applications, Allied Publishers, 1996.
- 2. A. Kaufman, Introduction to the theory of Fuzzy Subsets, Academic Press, 1975.
- 3. V. Novak, Fuzzy Sets and their Applications, Adam Hilger, Bristol, 1969.

E-Materials:

http://nptel.ac.in/courses/105108081/module9/lecture36/lecture.pdf

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COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	S	L	S	S	L	L
CO2	S	S	М	М	S	L	S	S	L	L
CO3	S	S	М	М	S	L	S	S	L	L
CO4	S	S	М	М	S	L	S	S	L	М
CO5	S	S	S	S	S	L	S	S	М	М

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II	Paper type : Core Elective	Credit : 3
Paper code :	Name of the Paper : Difference Equations	
Hours of Teaching:75hrs		

Course Objectives:

The main objectives of the course are to

- 1. To provide basic knowledge about the discretization process, the discrete version of difference equations.
- 2. Understand the Linear periodic systems.
- 3. Develop the students ability todifferenceequationsusingZ-transforms.
- 4. To enable to use of OscillationTheory.
- 5. Study oscillation and asymptotic behavior of solutions of certain classes of difference equations.

CourseLearningOutcomes:

Afterthesuccessful completion of this course, the students will be able to:

- CO1 Solveproblemson Linear DifferenceEquationsofHigherorder.
- CO2 Understand the system of Linear Difference Equations.
- CO3 Apply Z-transformtechniques indifference equations.
- CO4 Explain onOscillation Theory.
- CO5 Discuss on Asymptotic Behavior of Difference Equation.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	Yes
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	Yes

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Unit – 1 LinearDifferenceEquationsof Higherorder

DifferenceCalculus-GeneralTheoryofLinearDifferenceEquations-LinearHomogeneous Equations with Constant coefficients - Non-homogeneous equations: Methodof Undetermined Coefficients, the method of variation of constants - Limiting behavior of Solutions.

Chapter2: Sections 2.1 to 2.5

Unit -2Systemof LinearDifferenceEquations

Autonomous Systems - The Basic Theory - The Jordan form - Linear periodic systems. Chapter3: Sections3.1to 3.4

Unit -3**TheZ-transformMethod**

DefinitionsandExamples,PropertiesofZ-transform-TheInverseZ-transformandSolutions of Difference Equations: Power series method, partial fraction method, the inverse integral method -Volterra Difference Equation of convolution type - Volterra Systems. Chapter6: Sections 6.1to 6.3, 6.5

Unit – 4 **OscillationTheory**

Three-termdifferenceEquations-Self-AdjointSecondOrderEquations-NonlinearDifference Equations.

Chapter7: Sections7.1 to 7.3

Unit – 5 AsymptoticBehaviourof DifferenceEquation 15 hours

Tools of Approximation - Poincare's Theorem - Asymptotically Diagonal Systems - High-Order Difference Equations - Second Order Difference Equations.

Chapter 8: Sections 8.1to 8.5

Text Book:

SaberN.Elaydi, An Introduction to Difference Equations, Third Edition, Springer Verlag, New York, 2005(FirstIndian Reprint 2008).

ReferenceBooks:

- 1. RonaldE.Mickens, *DifferenceEquationsTheory*, *ApplicationsandAdvancedTopics*, Third Edition, CRC Press, NewYork, 2015.
- 2. R.P.Agarwal., *DifferenceEquationsandInequalities*, MarcelDekker, 1999.
- 3. S.Goldberg, Introduction to Difference Equations, Dover Publications, 1986

45

15 hours

15 hours

15 hours

- 4. V.LakshmikanthamandTrigiante,*TheoryofDifferenceEquationsNumericalMethodsand Applications*,Second Edition, AcademicPress, New York,1988.
- 5. WalterG.Kelly,AllanC.Peterson,*DifferenceEquations*,*AnIntroductionwithApplications*, Academic Press, NewYork, 2001(FirstIndianReprint2006).

E-Materials:

- 1. http://people.math.aau.dk/~matarne/11-imat/notes2011a.pdf,
- 2. http://pj.freefaculty.org/guides/stat/Math/DifferenceEquations/DifferenceEquationsguide.pdf

Mapping with Learning Outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	Μ	S	Μ	L	Μ	S	L	S	L
CO2	Μ	S	Μ	S	S	Μ	Μ	S	L	Μ
CO3	S	S	L	S	L	S	S	Μ	L	L
CO4	Μ	L	Μ	L	S	Μ	Μ	S	Μ	S
CO5	S	Μ	S	S	Μ	L	Μ	L	L	Μ

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II	Paper type : Open Elective	Credit	:	3
Paper code :	Name of the Paper : Fundamentals of Insuran	ce		
Hours of Teaching:75hrs				

Course Objectives:

The main objective of this course are to:

- 1 Introduce the concept of insurance.
- 2 Study about the Life Insurance and claims.
- 3 Understand the concepts of Fire and Marine insurance.
- 4 Know about motor and other insurances.
- 5 Get the knowledge of getting job in insurance companies.

Course Outcomes

After successful completion on the course the student will be able to

- CO1 understand the principles and regulations of Insurance
- CO2 analyse the benefits of life insurance policies
- CO3 discuss the fire and marine insurance and its benefits
- **CO4** analyse the various insurance sectors
- CO5 Understand the duties of an insurance agent and procedure to get license.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	No	No
2	Yes	Yes	Yes	No	No	No
3	Yes	Yes	Yes	Yes	No	No
4	Yes	Yes	Yes	Yes	No	No
5	Yes	Yes	Yes	Yes	No	No

Unit – 1 Introduction to Insurance

Meaning, Definition of insurance- General principles of insurance - Types of insurance life, fire and marine-Difference between life and other types of insurance, Growth & Development of Indian insurance industry- Regulations of insurance business and the emerging scenario.

Unit – 2 Life Insurance

Introduction to life insurance : Features of life insurance-Essentials of life insurance, Different types of life policies- Annuities, Formation of life insurance contracts-Assignment and nominations- Lapses and revivals of policies. Surrender value, paid up value, Loans-Claims-Procedure for claims- Settlement of claims- Death and Maturity.

Unit – 3 Fire and Marine Insurance

Fire Insurance- Fire insurance contracts- Fire insurance coverage- Policies for stocks- Rate fixation in fire insurance- Settlement of claims. Marine Insurance- Functions- Marine perils-Types of marine policiesClauses in general use-Warranties and conditions- proximate cause-subrogation and conciliation - Reinsurance- Double insurance-Types of marine losses.

Unit – 4 Miscellaneous Insurance

Motor insurance - Employer's liability insurance - Personal accident and sickness insurance - Aviation insurance - Burglary insurance - Fidelity guarantee insurance - Engineering insurance crop insurance.

Unit – 5 Role of Insurance Agent

Procedure for becoming an Agent- Pre-requisite for obtaining a license- Duration of license-Cancellation of license- Termination of agency - Code of Conduct- Functions of the Agent.

Text book :

- 1. Fundamentals of Insurance Dr. Periyasamy, Himalaya Publishing Pvt Ltd, Mumbai.
- 2. Insurance principles and practice Moorthy. A, Margham publications, Chennai.
- 3. Fundamentals of insurance Dr. P. K. Guptha, Margham publications, Chennai

48

15 hours

15 hours

15 hours

15 hours

Reference Books:

- 1 Insurance principles and practice- Periasamy. P, Margham publications, Chennai
- 2 Insurance principles and practice Mishra. M. N, Sultan Chand & Sons, NewDelhi
- 3 Insurance principles and practice- Balu. V. & Premilan, Margham publications, Chennai

E-Materials:

- <u>https://ocw.mit.edu/courses/economics/14-73-the-challenge-of-world-poverty-spring-</u> 2011/video-lectures/lecture-15-risk-and-insurance/
- https://ocw.mit.edu/courses/economics/14-73-the-challenge-of-world-poverty-spring-2011/video-lectures/lecture-16-insurance/

Mapping with Learning outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	Μ	Μ	L	Μ	S	S	S	S	L	М
CO2	Μ	Μ	Μ	Μ	S	S	S	S	L	Μ
CO3	Μ	L	L	S	S	S	S	S	L	Μ
CO4	Μ	Μ	L	Μ	S	S	S	S	L	Μ
CO5	S	Μ	Μ	S	S	S	S	S	L	Μ

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II	Paper type : Open Elective	Credit : 3
Paper code :	Name of the Paper : NumericalMethods	
Hours of Teaching: 75hrs		

CourseObjectives:

Theobjectives of the courseisto

- 1. Understandtheconceptof solving algebraic and transcendental equations.
- 2. Studythevarious methods to obtain interpolation with equal and unequal intervals.
- 3. Get knowledge about numerical differentiation.
- 4. Demonstrate the numerical integration.
- 5. Solve the ordinary differential equations using various numerical methods.

Course Outcomes:

After successful completion on the course the student will be able to

- CO1 Solve algebraic and transcendental equations.
- **CO2** Acquire the knowledge of interpolation for equal and unequal intervals.
- CO3 Enrich the students to work effectively on numerical differentiation.
- CO4 Provides a foundation in the study of numerical integration.
- CO5 Knows to solve ordinary differential equations using various numericalmethods.

Matching Table

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1 Solutionofnumerical algebraic and transcendental Equations

Bisection method – Iteration Method – Newton-Raphson methodSolutionof simultaneouslinear algebraicequations:Gausseliminationmethod–Gauss-Jordaneliminationmethod–GaussJacobimethod–GaussSeidel method – Simple Problems.

Chapter3: Sections 3.1,3.1.1, 3.2, 3.4

Chapter4: Sections4.1, 4.2, 4.2.1, 4.8, 4.9.

Unit – 2 Interpolation

Introduction – Newton's forward and backward formulae – Central differences – Gaussforward and backward formulae – Stirling's formula – Divided differences – Properties – Relationsbetweendivided differences and forward differences. Newton's divided differences formula – Lagrange's formula.

Chapter6: Sections 6.1,6.2, 6.3

Chapter7: Sections 7.1,7.3, 7.4, 7.5

Chapter8: Sections 8.2, 8.3, 8.4, 8.5, 8.7

Unit – 3 NumericalDifferentiation

Newton'sforwardandbackwardformulaetocomputethederivatives–Derivativeusing Stirling's formulae – to find maxima and minima of the function given the tabularvalues. **Chapter9:** Sections 9.2,9.3, 9.4, 9.6

Unit - 4NumericalIntegration15 hoursNewton - Cote's formula - Trapezoidal rule - Simpson's 1/3rd and 3/8th rules - Weddlerule.rule.Chapter9: Sections 9.8, 9.9, 9.13, 9.14, 9.15

Unit – 5 Numerical solution of ordinary differential equations

Euler'smethod-ImprovedEuler'smethod-Modified Euler'smethod-Runge-Kutta method (Fourth orderonly).

Chapter11: Sections 11.9, 11.10, 11.11, 11.12, 11.13.

Text Book:

Kandasamy. P, Thilagavathi. K and Gunavathi. K "Numerical methods" – S. ChandandCompanyLtd, NewDelhi– ThirdRevised Edition 2016.

15 hours

15 hours

15 hours

ReferenceBooks:

- 1. Venkataraman M. K.,"Numerical Methods in Science and Engineering" NationalPublishingcompanyV Edition 1999.
- Sankara Rao K., "Numerical Methods for Scientists and Engineers" 2nd EditionPrenticeHallIndia 2004.
- 3. GuptaB.D., Numerical Analysis, Konark Publishers Pvt. Ltd.

E-Materials:

- 1. http://nptel.ac.in/courses/122102009/
- 2. http://www.math.ust.hk/~machas/numerical-methods.pdf
- 3. <u>https://mathworld.wolfram.com/</u>

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	Μ	S	S	S	S
CO2	S	S	Μ	Μ	S	М	S	S	S	S
CO3	S	S	М	М	S	М	S	S	S	S
CO4	S	S	М	М	S	М	S	S	S	S
CO5	S	S	Μ	Μ	S	М	S	S	S	S

Mapping with Programme Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : II	Paper type : Open Elective	Credit	:	3
Paper code :	Name of the Paper : Fundamentalsof Busines	ssStatistics	5	
Hours of Teaching: 75hrs				

CourseObjectives:

The main objective of this course are to:

- 1 Provide basic knowledge of the origin and evolution of Statistics
- 2 Applystatisticaltechniquesforinterpretinganddrawingconclusionforbusiness problems.
- 3 Develop the students ability to deal with numerical and quantitative issues in business
- 4 Enable the use of statistical, graphical and algebraic techniques where ever relevant
- 5 Have a proper understanding of Statistical applications in Economics and Management.

CourseOutcomes

Aftersuccessful completion of the course the student will be able to

- CO1 ClassifyaboutthePartialandMultiple Correlation
- CO2 Explain the basic concepts of Probability and Theoretical Distributions
- CO3 Identify the educated guess (hypothesis)

CO4 Analyzethestatisticalinferences-TestofHypothesis,Chisquareand goodness of

Fit and F-Test

CO5 Discuss and designtheAnalysisofVariance

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	No
2	Yes	Yes	No	No	Yes	No
3	Yes	Yes	Yes	No	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	No	Yes	Yes	Yes

Matching Table:

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Unit – 1 PartialandMultipleCorrelation

Introduction-PartialCorrelation-MultipleCorrelation-MultipleRegressionAnalysis-ReliabilityofEstimates-MiscellaneousIllustrations

Volume–II:Chapter9:Pages:1109to1135

Unit – 2 Theoryof ProbabilityandTheoreticalDistributions

Introduction–ProbabilityDefined–ImportanceoftheConceptofProbability– CalculationofProbability–TheoremsofProbability-ConditionalProbability-Bayes'theorem– ProbabilityDistribution–BinomialDistribution-PoissonDistribution. Volume–II:Chapter1:Pages:751to770and774to788; Chapter2:Pages:806to823,826to833and 858 to 879

Unit – 3 StatisticalInference-TestofHypothesis

Introduction–SamplingErrorandSamplingDistribution–Estimation– TestofSignificanceforLargeSamples–TestofSignificanceforSmallSamples-MiscellaneousIllustrations.

Volume–II: Chapter 3:Pages: 882 to 951)

Unit – 4 ChisquareandGoodnessofFit

Introduction-Chisquaredefined–ConditionsofAdditiveChi-SquareTest–Yate'sCorrections-UsesofChi-SquareTest–AdditivePropertyofChi-Square–Chi-SquareTestforSpecifiedValueofPopulationVariance–MiscellaneousIllustrations. Volume–II:Chapter 4: Pages: 953to 1003

Unit – 5 F-Testand AnalysisofVariance

The F TestortheVarianceRatioTest-ApplicationF Test-AnalysisofVariance-

Assumptions In Analysis of Variance-Technique of Analysis of Variance-Coding data-Coding data-Coding

Analysis of Variance in Two-Way Classification Model.

Volume-II:Chapter5:Pages:1006 to 1038

Text Book:

S.P. Gupta, Statistical Methods, Sultan Chand & Sons, New Delhi, 2009.

54

15 hours

15 hours

15 hours

15 hours

ReferenceBooks:

- 1. S.C.GuptaandV.K.Kapoor,FundamentalsofMathematicalStatistics,11e,SultanChand&Sons, NewDelhi, 2004.
- S.P.Gupta&M.P.Gupta,BusinessStatistics,14thenlargededition,SultanChand&Sons, Educational publishers, New Delhi, reprint 2007.
- 3. RichardILevinandDavidS.Rubit,StatisticsforManagement,Seventhedition,PearsonEduc ation, NewDelhi, 2002.
- 4. P.R.Vittal,BusinessMathematicsandStatistics,MarghamPublications,Sixthrevisededitio n, 2011.

E-Materials:

http://mathworld.wolfram.com

Mapping with Learning Outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	L	S	S	S	Μ	S
CO2	S	S	Μ	Μ	S	S	S	S	Μ	S
CO3	S	S	Μ	S	S	S	S	S	Μ	S
CO4	S	S	S	Μ	Μ	S	S	S	Μ	S
CO5	S	S	Μ	Μ	S	S	S	S	Μ	S

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115 M.Sc. Mathematics – 2022-2023 Onwards

Semester : III

Paper Type : Core

Credit : 6

Paper Code :

Name of the Paper : Complex Analysis – I

Hours of Teaching : 90 Hours

Course Objectives

The objectives of this course are to

- 1 Introduce the notions of differentiability, analyticity and power series.
- 2 Discuss the complex integration, Cauchy theorem and its properties.
- 3 Educate the conformal mappings and Mobius transformations.
- 4 Inculcate the concepts of maximum principle, Schwarz's lemma and Liouville's theorem.
- 5 Indoctrinate the singularities and its classification.

Course Outcomes

After the successful completion of this course, the students will be able to

- CO1 Understand the notions of differentiability, analyticity, power series and its consequences.
- CO2 Comprehend the complex integration, Cauchy theorem and its properties.
- CO3 Know the conformal mappings and Mobius transformations.
- CO4 Acquire the concepts of maximum principle, Schwarz's lemma and Liouville's theorem.
- **CO5** Procure the singularities and its classification.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	No	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	No	No
4	Yes	Yes	Yes	No	No	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1: Analytic Functions and Power Series

Differentiability and Cauchy-Riemann Equations – Harmonic Functions – Power Series as an Analytic Function – Exponential and Trigonometric Functions – Logarithmic Functions – Inverse Functions.

Chapter 3: Sections: 3.1 to 3.6

Unit – 2: Complex Integration

Curves in the Complex Plane – Properties of Complex Line Integrals – Cauchy-Goursat Theorem – Consequence of Simply Connectivity – Winding Number or Index of a Curve – Cauchy Integral Formula – Taylor's Theorem – Zeros of Analytic Functions – Laurent Series. **Chapter 4:** Sections: 4.1 to 4.5, 4.7, 4.10 to 4.12

Unit – 3: Conformal Mappings and Mobius Transformations

Principle of Conformal Mapping – Basic Properties of Mobius Maps – Fixed Points and Mobius Maps – Triples to Triples under Mobius Maps – The Cross-Ratio and its Invariance Property – Conformal Self-maps of Disks and Half-planes.

Chapter 5: Sections: 5.1 to 5.6

Unit – 4: Maximum Principle, Schwarz's Lemma and Liouville's Theorem 18 Hours

Maximum Modulus Principle - Hadamard's Three Circles/Lines Theorems - Schwarz's Lemma and its Consequences - Liouville's Theorem - Doubly Periodic Entire Function - Fundamental Theorem of Algebra - Zeros of Certain Polynomials.

Chapter 6: Sections: 6.1 to 6.7

Unit – 5: Classification of Singularities

Isolated and Non-isolated Singularities – Removable Singularities – Poles – Further Illustrations through Laurent's Series – Isolated Singularities at Infinity – Meromorphic Functions – Essential Singularities and Picard's theorem.

Chapter 7: Sections: 7.1 to 7.7

Text Book:

S. Ponnusamy, *Foundations of Complex Analysis*, Second Edition, Narosa Publishing House, New Delhi, 2012.

57

18 Hours

18 Hours

18 Hours

18 Hours

Reference Books:

- 1. Lars V. Ahlfors, *Complex Analysis*, 3rd Edition, McGraw-Hill Inc., New York, 1979.
- 2. J.W. Brown and R.V. Churchill, *Complex Variables and Applications*, 8th Edition, McGraw-Hill Higher Education, New York, 2009.
- J.B. Conway, *Functions of One Complex Variable*, 2nd Edition, Narosa Publishing House, New Delhi, 1996.
- 4. V. Karunakaran, *Complex Analysis*, 2nd Edition, Narosa Publishing House, New Delhi, 2005.
- 5. H.A. Priestley, *Introduction to Complex Analysis*, 2nd Edition, Oxford University Press Inc., New York, 2005.

E-Materials:

- 1. <u>https://nptel.ac.in/courses/111106141</u>
- <u>https://ocw.mit.edu/courses/mathematics/18-04-complex-variables-with-applications-spring-</u>2018/
- 3. https://www.coursera.org/learn/complex-analysis

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	М	S	S	S	S	S
CO2	S	S	М	М	М	S	S	S	S	S
CO3	S	S	М	М	М	S	S	S	S	S
CO4	S	S	М	М	М	S	S	S	S	S
CO5	S	S	М	М	М	S	S	S	S	S

Mapping with Programme Outcomes

*PO – Programme Outcome, CO – Course Outcome.

THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115

M.Sc. Mathematics – 2022-2023 Onwards

Semester : III

Paper Code :

Paper Type : Core

Credit : 5

Name of the Paper : Topology

Hours of Teaching : 90 Hours

Course Objectives

The objectives of this course are to

- 1 Introduce the mathematical analysis of open and closed sets and the significance of the topological spaces.
- 2 Discuss about the continuous functions on topological spaces, product topology and topology induced by the metric.
- 3 Educate the connected spaces, connected subspaces, components and local connectedness.
- 4 Inculcate the notions of compactness, compact subspaces, limit point compactness and local compactness.
- 5 Indoctrinate the strong theoretical background about the countability axioms, the separation axioms and the consequences theorems.

Course Outcomes

After the successful completion of this course, the students will be able to

- **CO1** Know the basics on open and closed sets and the significance of the topological spaces.
- **CO2** Comprehend the continuous functions on topological spaces, product topology and topology induced by the metric.
- CO3 Understand the connected spaces, connected subspaces, components and local connectedness.
- **CO4** Acquire the notions of compactness, compact subspaces, limit point compactness and local compactness.
- **CO5** Procure the strong theoretical background about the count ability axioms, the separation axioms and the consequences theorems.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	No	No
2	Yes	Yes	Yes	Yes	No	No
3	Yes	Yes	Yes	Yes	No	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Matching Table:

59

Unit-1: **Topological Spaces**

Topological Spaces – Basis for a Topology – The Order Topology – The Product Topology on $X \times Y$ - The Subspace Topology - Closed Sets and Limit Points. Chapter 2: Sections 12–17

Unit-2: **Continuous Functions**

Continuous Functions – The Product Topology – The Metric Topology. Chapter 2: Sections 18–21

Unit-3: **Connectedness 18 Hours**

Connected Spaces – Connected Subspaces of the Real Line – Components and Local Connectedness. Chapter 3:Sections 23–25

Unit-4: **Compactness**

Compact Spaces - Compact Subspaces of the Real Line - Limit Point Compactness - Local Compactness.

Chapter 3:Sections 26–29

Unit-5: **Countability and Separation Axioms**

The Countability Axioms - The Separation Axioms - Normal Spaces - The Urysohn Lemma -TheUrysohnMetrization Theorem - The Tietz Extension Theorem.

Chapter 4:Sections 30–35

Text Books:

James R. Munkres, *Topology*, 2nd Edition, Pearson Education Pvt. Ltd., Delhi, 2002.

Reference Books:

- 1. J. Dugundji, *Topology*, Prentice Hall of India Pvt. Ltd., New Delhi, 1975.
- 2. G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw Hill Education, New York, 1963.
- 3. J.L. Kelley, General Topology, Van Nostrand Reinhold Company, New York, 1955.
- 4. L.A. Steen and J.A. Seebach, Counterexamples in Topology, Holt, Rinechart and Winston, New York. 1970.
- 5. S. Willard, General Topology, Addison–Wesley Publishing Company, USA, 1970.

60

18 Hours

18 Hours

18 Hours

18 Hours

E-Materials:

- 1. <u>https://ocw.mit.edu/courses/mathematics/18-901-introduction-to-topology-fall-2004/index.htm</u>
- 2. <u>https://ocw.mit.edu/courses/mathematics/18-904-seminar-in-topology-spring-2011/index.htm</u>
- 3. <u>https://swayam.gov.in/nd2_cec20_ma12/preview</u>

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
C01	S	S	М	М	М	S	S	S	S	S
CO2	S	S	М	М	М	S	S	S	S	S
CO3	S	S	М	М	М	S	S	S	S	S
CO4	S	S	М	М	М	S	S	S	S	S
CO5	S	S	М	М	М	S	S	S	S	S

Mapping with Programme Outcomes:

*PO – Programme Outcome, CO – Course Outcome.

THIRUVALLUVAR UNIVERSITY, VELLORE - 632115

M.Sc. Mathematics - 2022 - 2023 onwards

Semester : III

Paper code :

Paper type : Core

Credit : 5

Name of the Paper : Differential Geometry

Hours of Teaching:90 hrs

Course Objectives:

The main objective of this course are to:

- 1 Introduce space curves and its characterizations.
- 2 Study properties of curves on surfaces.
- 3 Understand the concepts of Geodesics and canonical Geodesics equations.
- 4 Teach some type of special surfaces such as Developable and Minimal surfaces.
- 5 Get the knowledge on differential geometry of surfaces.

Course Outcomes

After successful completion on the course the student will be able to

- **CO1** Understand the concept of a space curve and compute its curvature and torsion.
- CO2 Acquire the knowledge of curves on a surface and its intrinsic properties.
- CO3 Analyze the geodesics and its normal properties and also familiar with Gauss Bonnet Theorem.
- CO4 Determine the second fundamental form and developable associated with space curves.
- CO5 Know Hilbert's Lemma and the fundamental existence theorem for surface theory.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating	
1	Yes	Yes	No	No	Yes	No	
2	Yes	Yes	No	No	Yes	No	
3	Yes	Yes	Yes	Yes	Yes	No	
4	Yes	Yes	Yes	Yes	Yes	No	
5	Yes	Yes	Yes	Yes	Yes	No	



Unit - 1 **Space Curves**

Definition of a space curve - Arc length - Tangent - Normal and binormal - Curvature and torsion - Contact between curves and surfaces - Tangent surface - Involutes and evolutes intrinsic equations – Fundamental existence theorem for space curve – Helices. Chapter 1: Sections 1 to 9

Unit - 2 Intrinsic Properties of a Surface Definition of a surface - Curves on a surface - Surface of revolution - Helicoids - Metric -

Direction coefficients - Families of curves - Isometric correspondence - Intrinsic properties. Chapter 2: Sections 1 to 9

Unit - 3 Geodesics

Geodesics – Canonical geodesic equations – Normal properties of geodesics – Existence theorem - Geodesic parallels - Geodesic curvatures - Gauss Bonnet theorem - Gaussian curvature -Surface of constant curvature.

Chapter 2: Sections 10 to 18

Unit - 4 **Non–Intrinsic Properties of a Surface**

The second fundamental form - Principal curvature - Lines of curvature - Developable -Developable associated with space curves and with curves on surface - Minimal surfaces -Ruled surfaces.

Chapter 3: Sections 1 to 8

Unit - 5 **Differential Geometry of Surfaces**

Fundamental equations of surface theory - Fundamental existence theorem for surfaces -Compact surfaces whose points are umbilics- Hilbert's lemma - Compact surfaces of constant curvature - Complete surfaces.

Chapter 3: Sections 9 to 11

Chapter 4: Sections 1 to 5

Text book :

T.J.Willmore, An Introduction to Differential Geometry, Oxford UniversityPress,(17th Impression) New Delhi 2002. (Indian Print)

18 hours

18 hours

18 hours

18 hours

Reference Books:

- 1. Struik, D.T. Lectures on Classical Differential Geometry, Addison Wesley, Mass. 1950.
- 2. Kobayashi. S. and Nomizu. K. Foundations of Differential Geometry, Interscience Publishers, 1963.
- 3. Wilhelm Klingenberg: A course in Differential Geometry, Graduate Texts in Mathematics, Springer-Verlag 1978.
- 4. J.A. Thorpe Elementary topics in Differential Geometry, Under graduate Texts in Mathematics, Springer Verlag 1979.

E-Materials:

http://www.math.ku.dk/noter/filer/geom1.pdf

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	L	М	S	L	S	S	L	М
CO2	S	S	М	L	S	L	S	S	М	М
CO3	S	S	М	М	S	L	S	S	М	М
CO4	S	S	М	М	S	L	S	S	М	М
CO5	S	S	М	М	S	L	S	S	М	М

Mapping with Learning outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE - 632115

M.Sc. Mathematics - 2022 - 2023 onwards

Semester	:	III	
Paper cod	e:		
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Paper type : Core Elective Name of the Paper : LaTeX

Credit : 3

Hours of Teaching: 90hrs

Course Objectives:

The main objective of this course are to:

- 1 Inculcate the computer knowledge.
- 2 Introduce the LaTeXsoftware
- 3 Train in the Preparation of Project and dissertations using LaTex.
- 4 Educate the Latex coding.
- 5 Understand the concepts of Cross References, Footnotes, Margin pars and Endnotes

Course Outcomes

After successful completion on the course the student will be able to

- **CO1** Understand the basic LaTeX document and the e-contents.
- CO2 Construct the structures of contents, index, glossary and text.
- **CO3** Create the type setting equations
- CO4 Discuss several types of boxes and floats.
- CO5 Prepare the basic documentation

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating	
1	Yes	Yes	No	No	No	Yes	
2	Yes	Yes	Yes	No	No	Yes	
3	Yes	Yes	No	No	No	Yes	
4	Yes	Yes	No	No	No	Yes	
5	Yes	Yes	Yes	No	No	Yes	

Unit - 1 Basic Document and Bibliography

Whats is LATEX – Simple typesetting – Fonts Type size – Document class – page style – page numbering – Formatting lengths – parts of a document – Dividing the document – what next? – Introduction – natbib – The BIBTEX program – BIBTEX Style files – Creating a bibliographic database.

Chapter: 1 to 4

Unit - 2 Contents, Index, Glossary, Text, Row and Column

Table of contents – Index – Glossary. Borrowed words – Poetry in typing – Making lists – When order matters – Description and definitions.

Chapter: 5 to 6

Unit - 3Typesetting Equations and Theorems18 hoursKeeping tabs – Tables – The basics – Custom commands – More on mathematics – mathematicsmiscellany – New operations – The many fact of mathematics – Symbols – Theory in LATEX –Designer theorem-the amsthm package – Housekeeping.Chapter: 7 to 9

Unit - 4Several Kinds of boxes and Floats,18 hoursLR boxes - Paragraph boxes - Paragraph boxes with specific height - Nested boxes - Roleboxes - The figure environment - The table environment.Chapter: 10 to 11

Unit - 5Cross References in LATEX, Footnotes, Marginpars and
Endnotes18 hours

Why cross reference? – Let LATEX do it – Pointing to a page-the package varioref – Pointing outside-the package xr – Lost the keys? Use lables.tex – Footnotes – Marginal notes – Endnotes. **Chapter:** 12 to 13

Text book :

A Primer, Latex Tutorials, Indian TEX users group, Trivandrum, India. <u>www.tug.org.in</u>

66

18 hours

Reference Books:

- Peter Flynn, A beginner's introduction to typesetting with LATEX, Silmaril Consultants, Textual Therapy Division, 2003.
- 2. George Gratzer, More Math Into LATEX, 4th Edition, Springer Science (2007).
- Frank Mittelbach, Michel Goossens, The LaTex Companion, Second Edition, Addison-Wesley, 2004.

E-Materials:

- 1. <u>https://www.latex-tutorial.com/tutorials/</u>
- 2. https://www.latex-tutorial.com/
- 3. <u>http://www.tug.org.in/tutorials.html</u>

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	М	L	L	М	S	L	S	S	М
CO2	S	М	L	М	М	L	L	S	S	М
CO3	S	L	L	М	L	L	L	S	S	М
CO4	S	L	L	L	М	L	L	S	S	М
CO5	S	L	L	М	L	L	L	S	S	S

Mapping with Learning outcomes:

* PO – Programme Outcome, CO – Course Outcomes
THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115

M.Sc. Mathematics – 2022-2023 Onwards

Semester : III

Paper Type : Core ElectiveCredit : 3

Paper Code :

Name of the Paper : Discrete Mathematics

Hours of Teaching : 90 Hours

Course Objectives

The objectives of this course are to

- 1 Introduce the algebraic structures of lattices and Boolean algebra.
- 2 Construct the switching circuits with applications.
- 3 Educate the finite fields and its mathematics properties.
- 4 Inculcate the polynomials over finite fields, Irreducibility and factorization of polynomials.
- 5 Indoctrinate the coding theory with the linear and cyclic codes.

Course Outcomes

After the successful completion of this course, the students will be able to

- **CO1** Know the algebraic structures of lattices and Boolean algebra, and sketch the minimization of Boolean polynomials.
- **CO2**Model the switching circuits with applications.
- CO3 Understand the finite fields and its mathematics properties.
- **CO4** Acquire the notions of the polynomials over finite fields, Irreducibility and factorization of polynomials.

CO5Apply the coding theory with the linear and cyclic codes in cryptography.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	Yes	No
2	Yes	Yes	Yes	No	No	No
3	Yes	Yes	No	Yes	Yes	No
4	Yes	Yes	No	Yes	Yes	No
5	Yes	Yes	Yes	No	No	No

Unit-1: Lattices

Properties and Examples of Lattices – Distributive Lattices – Boolean Algebras – Boolean Polynomials - Minimal Forms of Boolean Polynomials. Chapter 1: Sections 1–6

18 hours

18 hours

Unit-2 :Applications of Lattices18 hoursSwitching Circuits – Applications of Switching Circuits.

Chapter 2:Sections 7–8

Unit-3 :Finite Fields18 hoursFinite Fields.Chapter 3:Sections 13

Unit-4 :Polynomials18 hoursIrreducible Polynomials over Finite Fields - Factorization of Polynomials over Finite Fields.18 hoursChapter 3:Sections 14–1514–1514–15

Unit -5: Coding Theory Linear Codes – Cyclic Codes. Chapter 4:Sections 17–18

Text Books:

Rudolf Lidl and Gunter Pilz, *Applied Abstract Algebra*, 2nd Indian Reprint, Springer Verlag, NewYork, 2006.

Reference Books:

- 1. A.Gill, *Applied Algebra for Computer Science*, Prentice Hall Inc., New Jersey.
- J.L.Gersting, Mathematical Structures for Computer Science, 3rdEdn., ComputerScience Press, New York.
- 3. S.Wiitala, Discrete Mathematics A Unified Approach, McGraw Hill Book Co.

E-Materials:

- 1. <u>http://www.discrete-math-hub.com/resources-and-help.html</u>
- 2. <u>https://onlinecourses.nptel.ac.in/noc22_cs123/preview</u>
- 3. <u>https://onlinecourses.nptel.ac.in/noc22_cs85/preview</u>

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COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	М	S	S	S	S	S
CO2	S	S	М	М	S	S	S	S	S	S
CO3	S	S	М	М	М	S	S	S	S	S
CO4	S	S	М	М	М	S	S	S	S	S
CO5	S	S	М	М	S	S	S	S	S	S

Mapping with Programme Outcomes:

PO - Programme Outcome, CO - Course Outcome.

*S-Strong, M-Medium, L-Low.

THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115

M.Sc. Mathematics – 2022-2023 Onwards

Semester : III

Paper Type : Core ElectiveCredit : 3

Paper Code :

Name of the Paper : Operations Research

Hours of Teaching : 90 Hours

Course Objectives

Theobjectives of the course is to

- 1. Understand the steps in decisiontheoryandtreeanalysis
- 2. Make distinctions among various types of replacement and maintenance techniques.
- 3. Solve an LPP using dynamic programming approach..
- 4. Use differential calculus based methods to obtain the optimal solutions.
- 5. Derive and use Kuhn-Tucker conditions necessary for optimal vaule of an objective function.

Course Outcomes:

After successful completion on the course the student will be able to

- **CO1** Make decision under various decision-making environments.
- **CO2** Acquire the knowledge of replacement analysis in handling problems like staffing problem and equipment renewal problem etc.
- **CO3** Work effectively on Dynamic Programming models and their applications in solving Decision problem.
- **CO4** Provide a strong foundation in distinction between local, global and inflection extreme points.
- **CO5** Solve non-linear programming problems.

Matching Table :

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

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Unit-1: **Decision Theory**

Steps in Decision theory Approach – Types of Decision Making Environments –DecisionMaking Under Uncertainty - Decision Making under Risk - Posterior Probabilities and Bayesian Analysis-DecisionTreeAnalysis-DecisionMakingwith Utilities.

Chapter11:Sections 11.1to 11.8

Replacement and Maintenance Models Unit-2:

FailureMechanismofitems-ReplacementofItemsDeteriorateswithTime-Replacementofitems that fail completely- other ReplacementProblems

Chapter17:Sections 17.1 to 17.5

Unit-3: **Dynamic Programming**

Introduction - Dynamic Programming Terminology - Developing Optimal Decision Policy -Dynamic Programming under Certainty – Dynamic Programming Approach for Solving LPP. Chapter 22:Sections 22.1 to 22.5

Unit-4: **Classical Optimization Methods 18 Hours**

Unconstrained Optimization -Constrained multivariable Optimization with Introduction inequality constraints - Problems.

Chapter 23:Sections 23.1 to 23.4

Unit-5: **Non-Linear Programming Methods 18 Hours** Introduction - General NLPP - Graphical Solution - Quadratic Programming - Problems. Chapter 24:Sections 24.1 to 24.4

Text Book:

J.K.Sharma, Operations Research Theory and Applications (SixthEdition), Trinity Press, Laxmi Publications Pvt. Ltd., NewDelhi, Reprint 2017.

ReferenceBooks:

- 1. F.S.HillierandJ.Lieberman, IntroductionToOperationsResearch, (Eighthedition), TataMc Graw Hill PublishingCompany, New Delhi, 2006.
- 2. C.Beightler, D.Phillips, and B.Wilde, Foundations of Optimization, (Secondedition), Prenti ceHall New York, 1979.

72

18 Hours

18 Hours

18 Hours

- 3. M.S.Bazaraa, J.J.Jarvis, and H.D.Sharall, JohnWileyand sons, New York, 1990.
- D.GrossandC.M.Harris,FundamentalsOfQueuingTheory[3rdEdition],WileyandSons, New York, 1998.
- 5. HamdyA.Taha,OperationsResearch,(Sixthedition),Prentice– HallofIndiaPrivateLimited,NewDelhi.

E-Materials:

https://onlinecourses.nptel.ac.in/noc19_ma29/prev https://archive.nptel.ac.in/courses/111/107/111107104/ https://onlinecourses.nptel.ac.in/noc21_mg74/preview https://mathworld.wolfram.com/topics/Optimization.html

Mapping with Programme Outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	Μ	S	S	S	S
CO2	S	S	Μ	Μ	S	Μ	S	S	S	S
CO3	S	S	Μ	Μ	S	Μ	S	S	S	S
CO4	S	S	Μ	Μ	S	Μ	S	S	S	S
CO5	S	S	Μ	Μ	S	Μ	S	S	S	S

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : III	Paper type : Open Elective	Credit	:	3		
Paper code :	Name of the Paper : Mathematical Biology					
Hours of Teaching : 90 Hours						

CourseObjectives:

The main objectives of the course are to

- 1. Understand and knowthediscretepopulationgrowthmodels.
- 2. Develop the Model for the Distribution of drugs in the body
- 3. Apply the Model for the Spread of Technological Innovations
- 4. Studythecontinuousgrowthmodelsand qualitativebehaviorofpopulations
- 5. Knowthemathematicalmodelsin epidemiology.

CourseLearningOutcomes

Afterthesuccessful completion of this course, the students will be able to:

CO1	Formulatethemathematicalmodelsforrealworldproblems
CO2	Understanding the concepts of Discrete Population Growth Models
CO3	DiscusstheContinuous Growth Models
CO4	Explain the Logistic Model with Harvesting
CO5	Analyze the Qualitative behavior of Populations and Mathematical Models
	in Epidemiology.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	Yes

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StructuredPopulations.	
Chapter2:Sections 2.2 to 2.5	
Unit-2:ContinuousGrowthModels	18hou
TheLinearModel-The ExponentialModel-Model for the Distribution of drugs in the body	
CoalitionModels.	
Chapter3:Sections 3.2 to 3.5	
Unit-3:ContinuousGrowthModels(contd.)	18 hou
Environmental Desistance A Model for the Spread of Technological	Innovation

Growth

Environmental Resistance - A Model for Technological Innovations the Spread ot TheGomertzModel -BertalanffyGrowth Model.

Chapter3:Sections 3.8 to 3.11

Arithmetic

Unit-4: Qualitative behavior of Populations

omous Equations - Steady and Equilibrium State - Stability of Equilibrium State - Logistic Model with Harvesting - Fixed Points and their stability - The Logistic Map.

Chapter5:Sections 5.2 to 5.7

Unit-5:MathematicalModelsinEpidemiology

Plant Epidemics - Some features of Human Epidemics - A Simple Deterministic EpidemicModel-A moreGeneralEpidemic: SIR Disease.

Chapter7:Sections 7.2 to 7.5

Text Book:

C.R.Ranganathan,

AFirstCourseinMathematicalModelsofPopulationGrowth(withMATLABProgram),

AssociatedPublishingCompany,NewDelhi,2006.

ReferenceBooks:

- 1. Pundir, BioMathematics, APragatiEdition, 2006.
- 2. J.N. Kapur, Mathematical Models in Biology and Medicine, Affiliated East-WestPressPvt.Ltd., NewDelhi, 1985.
- 3. Nicolas F. Britton, Essential Mathematical Biology, Springer InternationalEdition,FirstIndianreprint, 2004.

Growth Model _ Geometric

Unit-1:DiscretePopulationGrowthModels

18 hours Model Generalizations _ Age -

18hoursAuton

18hours

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4. Murray, MathematicalBiology, Springer InternationalEdition, FirstIndianreprint, 2004.

E-Materials:

- 1. <u>https://www.smb.org/</u>
- 2. https://web.archive.org/web/20080827161431/http://www.biostatsresearch.com/repository/

COs **PO1 PO2** PO3 **PO4 PO5 PO6 PO7 PO8 PO9 PO10 CO1** S S S S S L Μ Μ Μ Μ **CO2** S S L S L Μ Μ Μ \mathbf{M} Μ S S **CO3** Μ S L L S L Μ L S S **CO4** Μ L Μ Μ S L S Μ **CO5** S S Μ L S Μ Μ L L S

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IIIPaper type : Open ElectiveCredit : 3Paper code :Name of the Paper : QuantitativeTechniques

Hours of Teaching: 90hrs

CourseObjectives:

Theobjectives of the courseis to

- 1. Studythe linearprogrammingproblem and its solving method.
- 2. Understandthetransportationproblem as a linear programming problem.
- 3. Understand the concept of assignmentproblem.
- 4. Understand the concept of inventory control.
- 5. Know about the network analysis and its solution methods, PERT and CPM.

Course Outcomes:

After successful completion on the course the student will be able to

CO1Understand the concept of LPP and its solution.

CO2Acquire the knowledge of transportation problems.

CO3Work effectively on assignment models.

CO4 Provides a strong foundation in the study of thecharacteristics of inventory controls.

CO5Use PERT-CPMtechniqueforprojectmanagement network problems.

Matching Table :

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit-1:LinearProgrammingProblem

Introduction-GraphicalSolutionMethod-SomeExceptionalCases-GeneralLinearProgrammingProblem-FundamentalPropertiesofSolution-TheComputationalProcedure-SimplexMethod. Chapter3:Sections3.1to3.4 Chapter4:Sections4.1 to 4.3

Unit-2:TransportationProblem

Introduction -L.P Formulationof the Transportation Problem - Existence of Solution in T.P -Transportation Table- Solution of a Transportation Problem- Finding InitialBasicFeasibleSolution-Testforoptimality-EconomicInterpretationofu; 's-DegeneracyinTransportationProblem-TransportationAlgorithm(ModiMethod).

Chapter10: Sections 10.1 to 10.3, 10.5, 10.8 to 10.13

Unit–3:Assignment Problem

Introduction-MathematicalFormulationoftheProblem-SolutionMethodsofAssignmentProblem-SpecialCasesinAssignmentProblems-TravellingSalesmanProblem.

Chapter11:Sections 11.1 to 11.4, 11.7

Unit–4:Inventory Control

Introduction - Types of Inventories - Reasons for Carrying Inventories - The InventoryDecisions -Objective of Scientific Inventory Control -Costs Associated with Inventories -Factors Affecting with Inventory Control - An inventory Control Problem - DeterministicInventoryproblem withNo shortages.

Chapter 19:Sections 19.1 to 19.10

Unit-5:NetworkschedulingbyPERTandCPM

Introduction-Network:BasicComponents -LogicalSequencing-RulesofNetworkConstruction-ConcurrentActivities–CriticalPathAnalysis–ProbabilityConsiderationsinPERT-Distinction between PERT and CPM.

Chapter25

18 hours

18 hours

18hours

18 hours

18 hours

78

Text Book:

KantiSwarup, P.K.Gupta, ManMohan, Operations Research, Sultan Chand & Sons, New Delhi, 2008.

ReferenceBooks

- 1. P.K.Gupta, Operations Research, 8-e, Krishna Prakasam Mandir, Meerut, 1993.
- 2. P.K.GuptaandD.S.Hira,OperationsResearch,S.Chand&Company,NewDelhi,2000.
- J.K.Sharma,OperationsResearchTheoryandApplications,2-e,Mac MillianBusinessBooks, 2003.
- 4. HamdyA.Taha,OperationsResearch,PearsonEducation,NewDelhi,2002.

E-Materials:

https://mathworld.wolfram.com/ https://nptel.ac.in/courses/112106134

Mapping with Programme Outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
C01	S	S	Μ	Μ	S	Μ	S	S	S	S
CO2	S	S	Μ	Μ	S	Μ	S	S	S	S
CO3	S	S	Μ	Μ	S	Μ	S	S	S	S
CO4	S	S	Μ	Μ	S	Μ	S	S	S	S
CO5	S	S	Μ	Μ	S	Μ	S	S	S	S

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : III

Paper code :

Paper type : Open Elctive Name of the Paper : SCILAB Credit : 3

Hours of Teaching: 90hrs

Course Objectives:

The main objective of this course are to:

- 1 Understand the basic commands
- 2 Solve the system of equations
- 3 Construct the plotting lines and data.
- 4 Evaluate the polynomials
- 5 Solve the Ordinary differential equations.

Course Outcomes

After successful completion on the course the student will be able to

- CO1 Acquire the practical knowledge of SCILAB
- CO2 Understand the matrices, vectors in SCILAB
- CO3 Visualize the mathematical objects in 2D and 3D
- CO4 Acquire the knowledge of polynomials
- CO5 Obtain the solution of Ordinary Differential equations

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	Yes	Yes	Yes	Yes
3	Yes	Yes	Yes	Yes	Yes	Yes
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	No	Yes	No

Chapter 1: Sections 1.1 to 1.7	
Unit-2 Matrix Calculation	18 Hours

Login - Talking between Scilab and the Editor - Basic Commands - Linear Algebra - Loops and

Matrices and Vectors - Solving Equations - Creating Matrices - Systems of Equations. Chapter 2: Section 2.2

Unit-3 Data and Function Plots Plotting Lines and Data - Adding a Line - Hints for Good Graphs - Graphs - Function Plotting -Component Arithmetic - Printing Graphs - Saving Graphs.

Chapter 3: Sections 3.2, 3.3

Unit-1 Introduction to SciLAbB

Conditionals - Help in Scilab.

Unit-4 Polynomials

Evaluation of Polynomials - Polynomials - Linear Least Squares (Heath Computer Problem).

Chapter 6: Sections 6.2, 6.3, 6.4

Unit-5 Differential Equation

Differential Equations - Scalar ODE's - Order 2 ODE's.

Chapter 8: Sections 8.2

Text book :

Graeme Chandler and Stephen Roberts, Scilab Tutorials for Computational Science, 2002.

Reference Books:

- 1. Scilab for very beginners, Scilab Enterprises, S.A.S, 143, bis rue Yves Le Coz 78000 Versailles (France).
- 2. K. S. Surendran, SCILAB FOR DUMMIES, Version 2.6.
- 3. Some notes on SCILAB, Universit'e de Nice Sophia-Antipolis.

E-Materials:

https://www.scilab.org/

81

18 hours

18 hours

18 Hours

18 Hours

Cos	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	S	S	L	S	S	М	L
CO2	S	S	М	L	S	L	S	S	L	М
CO3	S	S	S	S	S	L	S	S	М	L
CO4	S	S	М	М	S	L	S	S	L	L
CO5	S	S	М	S	S	L	S	S	М	L

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115 M.Sc. Mathematics – 2022-2023 Onwards

Semester : IV

Paper Code :

Paper Type : Core

Credit : 4

Name of the Paper : Complex Analysis - II

Hours of Teaching : 75 Hours

Course Objectives

The objectives of this course are to

- 1 Introduce the concepts of residues and its properties.
- 2 Estimate the contour integrals and its applications.
- 3 Educate the analytic continuation and Poisson integral formula.
- 4 Inculcate the representations of meromorphic and entire functions.
- 5 Indoctrinate the applications of open mapping, Hurwitz and Riemann mapping theorems.

Course Outcomes

After the successful completion of this course, the students will be able to

- CO1 Understand the concepts of residues and its properties.
- **CO2** Evaluate the contour integrals and its applications.
- **CO3** Know the analytic continuation and Poisson integral formula.
- **CO4**Acquire the representations of meromorphic and entire functions.

CO5 Procure the applications of open mapping, Hurwitz and Riemann mapping theorems.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	Yes	No	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	No	No
4	Yes	Yes	Yes	Yes	No	No
5	Yes	Yes	Yes	Yes	Yes	No

Unit – 1: Calculus of Residues

Residue at a Finite Point – Residue at the Point at Infinity – Residue Theorem – Number of Zeros and Poles – Rouche's Theorem. Chapter 7: Sections 7.1 to 7.6 Chapter 8: Sections 8.1 to 8.5

Unit – 2: Evaluation of Certain Integrals

Integrals of three types - Singularities on the Real Axis - Integrals Involving Branch Points - Estimation of Sums.

Chapter 9: Sections 9.1 to 9.6

Unit – 3: Analytic Continuation

Direct Analytic Continuation - Monodromy Theorem - Poisson Integral Formula - Analytic Continuation via Reflection.

Chapter 10: Sections 10.1 to 10.4

Unit – 4: Representation of Meromorphic and Entire Functions 15 hours

Infinite Sums and Meromorphic Functions - Infinite Product of Complex Numbers - Infinite Products of Analytic Functions - Factorization of Entire Functions - The Gamma Function - The Zeta Function - Jensen's Formula - The Order and the Genus of Entire Functions. **Chapter 11:** Sections 11.1 to 11.8

Unit –5: Mapping Theorems

Open Mapping Theorem and Hurwitz' Theorem - Basic Results on Univalent Functions - Normal Families - The Riemann Mapping Theorem - Bieberbach Conjecture - The Bloch-Landau Theorems - Picard's Theorem.

Chapter 12: Sections 12.1 to 12.7

Text Books:

S. Ponnusamy, *Foundations of Complex Analysis*, Second Edition, Narosa Publishing House, New Delhi, 2012.

84

15 hours

15 hours

15 hours

15 hours

Reference Books:

- 1. Lars V. Ahlfors, *Complex Analysis*, 3rd Edition, McGraw-Hill Inc., New York, 1979.
- 2. J.W. Brown and R.V. Churchill, *Complex Variables and Applications*, 8th Edition, McGraw-Hill Higher Education, New York, 2009.
- 3. J.B. Conway, *Functions of One Complex Variable*, 2nd Edition, Narosa Publishing House, New Delhi, 1996.
- 4. V. Karunakaran, *Complex Analysis*, 2nd Edition, Narosa Publishing House, New Delhi, 2005.
- H.A. Priestley, *Introduction to Complex Analysis*, 2nd Edition, Oxford University Press Inc., New York, 2005.

E-Materials:

- 1. <u>https://nptel.ac.in/courses/111106141</u>
- <u>https://ocw.mit.edu/courses/mathematics/18-04-complex-variables-with-applications-spring-</u>2018/
- 3. https://www.coursera.org/learn/complex-analysis

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	М	S	S	S	S	S
CO2	S	S	М	М	М	S	S	S	S	S
CO3	S	S	М	М	М	S	S	S	S	S
CO4	S	S	М	М	М	S	S	S	S	S
CO5	S	S	М	М	М	S	S	S	S	S

Mapping with Programme Outcomes:

*PO – Programme Outcome, CO – Course Outcome.

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV

Paper code :

Paper type : Core

Credit : 4

Name of the Paper : Fluid Dynamics

Hours of Teaching: 75hrs

Course Objectives:

The main objective of this course are to:

- 1 Discuss kinematics of fluids in motion
- 2 Derive the equations of motion of a fluid
- 3 Introduce Three dimensional flows
- 4 Discuss Two dimensional image system
- 5 Analysis viscous flows

Course Outcomes

After successful completion of the course the student will be able to

- **CO1** Understand the concepts of kinematics of fluids in motions.
- CO2 Find the pressure at a point in a moving fluid.
- CO3 Discuss Stokes stream function.
- CO4 Analyse complex velocity potential for standard two dimensional flows.
- **CO5** Derive the Navier Stokes equations of motion of a Viscous fluid.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	No	No	No
2	Yes	Yes	Yes	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	No	Yes	Yes	No

Unit-1: **Kinematics of Fluids in Motion**

Real fluids and ideal fluids - Velocity of a fluid at a point, Stream lines, path lines, steady and unsteady flows - Velocity potential - The vorticity vector - Local and particle rates of changes -Equations of continuity – Worked examples – Acceleration of a fluid – Conditions at a rigid boundary.

Chapter 2: Sections 2.1 to 2.10

Unit-2: **Equations of Motion of Fluid**

Pressure at a point in a fluid at rest – Pressure at a point in a moving fluid – Conditions at a boundary of two inviscid immiscible fluids – Euler's equation of motion – Discussion of the case of steady motion under conservative body forces.

Chapter 3: Sections 3.1 to 3.7

Unit-3: **Some Three Dimensional Flows**

Introduction – Sources, sinks and doublets – Images in a rigid infinite plane – Axis symmetric flows - Stokes stream function.

Chapter 4: Sections 4.1, 4.2, 4.3, 4.5.

Unit-4: **Some Two Dimensional Flows**

Meaning of two dimensional flow - Use of Cylindrical polar coordinate - The stream function -The complex potential for two dimensional, irrational incompressible flow – Complex velocity potentials for standard two dimensional flows - Some worked examples - Two dimensional image systems – The Milne Thompson circle Theorem.

Chapter 5: Sections 5.1 to 5.8

Viscous Flows Unit-5:

Stress components in a real fluid - Relations between Cartesian components of stress -Translational motion of fluid elements – The rate of strain quadric and principal stresses – Some further properties of the rate of strain quadric - Stress analysis in fluid motion - Relation between stress and rate of strain - The co-efficient of viscosity and Laminar flow - The Navier -Stokes equations of motion of a Viscous fluid.

Chapter 8: Sections 8.1 to 8.9

15 hours

15 hours

15 hours

87

15 hours

15 hours

Text book :

F. Chorlton, Text Book of Fluid Dynamics, CBS Publications. Delhi ,1985.

Reference Books:

- 1. R.W.Fox and A.T.McDonald. Introduction to Fluid Mechanics, Wiley, 1985.
- 2. E.Krause, Fluid Mechanics with Problems and Solutions, Springer, 2005.
- 3. B.S.Massey, J.W.Smith and A.J.W.Smith, Mechanics of Fluids, Taylor and Francis, New York, 2005 4. P.Orlandi, Fluid Flow Phenomena, Kluwer, New Yor, 2002.
- 4. T.Petrila, Basics of Fluid Mechanics and Introduction to Computational Fluid Dynamics, Springer, berlin, 2004.

E-Materials:

http://web.mit.edu/1.63/www/lecnote.html

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	L	L	S	L	S	S	L	М
CO2	S	S	М	М	S	L	S	S	L	М
CO3	S	S	М	М	S	L	S	S	L	L
CO4	S	S	М	S	S	L	S	S	М	L
CO5	S	S	М	М	S	L	S	S	L	М

Mapping With Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV	Paper type : Core	Credit	:	5
Paper code :	Name of the Paper : Functional Analysis			

Hours of Teaching: 75hrs

CourseObjectives:

The main objective of this course are to:

- 1. Studythedetails of Banach SpacesandContinuous linear transformations
- 2. Get familiar with concepts of open mapping theorem also understand the properties of athogonal complements.
- 3. Provide the concept of conjugate space H*, adjoint, self-adjoint, normal and unitary operators.
- 4. Learn and understand the Preliminaries of Banachalgebras
- 5. Know about the structure of commutative Banach Algebras

CourseOutcomes:

Aftersuccessful completion of the course the student will be able to

- **CO1**Analysethe Banachspace with examples and Able to work comfortably with Continuous linear transformations
 - **CO2** Apply the conjugate operator and acquire the knowledge of openmappingtheorem.
- CO3 Discuss about the Hilbert spaces.
 - CO4 Acquire the knowledge of Banach Algebra and Outline of spectral radius.
 - **CO5** Construct the Gelfand-Neumark theorem.

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	No	Yes	No	No
2	Yes	Yes	Yes	Yes	No	No
3	Yes	Yes	No	No	Yes	Yes
4	Yes	Yes	No	No	Yes	No
5	No	Yes	No	Yes	No	No

Matching table:

UNIT-I:BanachSpaces

Definition - Some examples - Continuous Linear Transformations - The Hahn -BanachTheorem. Chapter 9: Sections 46 to 48

15 hours **UNIT-II:BanachSpacesAnd HilbertSpaces**

Open mapping theorem - conjugate of an operator - Definition and some simple properties -Orthogonal complements – Orthonormal.

Chapter 9: Sections 50 and 51

Chapter 10:Sections52, 53 and 54

UNIT-III:HilbertSpace

Conjugate space H* - Adjoint of an operator - Self-adjoint operator - Normal and UnitaryOperators-Projections.

Chapter10: Sections 55,56,57,58 and 59

UNIT-IV: Preliminaries of Banach Algebras

n and some examples - Regular and single elements - Topological divisors of zero -spectrumtheformula for the spectral radius-theradical and semi-simplicity.

Chapter12: Sections 64to 69

UNIT-V:StructureofCommutativeBanach Algebras 15hours

Gelfandmapping –Applicationsofthe formula $r(x) = \lim ||x^n||^{1/n}$ - Involutions inBanachAlgebras-

Gelfand-NeumarkTheorem.

Chapter13:Sections 70to73

Text Book:

. G.F.Simmons Introduction to topology and Modern Analysis, McGraw HillInternationalBook Company, NewYork, 1963.

ReferenceBooks:

- 1. W. Rudin Functional Analysis, Tata McGraw-Hill Publishing Company, New Delhi, 1973
- 2. G.Bachman&L.Narici, FunctionalAnalysis AcademicPress, NewYork, 1966.
- 3. H.C. Goffman and G.Fedrick, First course in Functional Analysis, Prentice Hall ofIndia, NewDelhi, 1987
- 4. E. Kreyszig Introductory Functional Analysis with Applications, John wiley& Sons.NewYork..1978.
- 5. BalmohanV.Limaye,LinearFunctionalAnalysisforScientistsandEngineers,Springer.

90

15 hours

15hoursDefinitio

15 hours

E-Materials

http://www.math.ucdavis.edu/~hunter/book/ch5.pdf

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	Μ	S	S	S	S	Μ	S
CO2	S	S	Μ	Μ	S	S	S	S	Μ	S
CO3	S	S	М	Μ	S	S	S	S	Μ	S
CO4	S	S	Μ	Μ	S	S	S	S	Μ	S
CO5	S	S	Μ	Μ	S	S	S	S	Μ	S

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV	Paper type : Core Elective	Credit	:	3
Paper code :	Name of the Paper : Number theory and Cryp	tography	7	
Hours of Teaching: 75hrs				

Course Objectives:

The main objective of this course are to:

- 1. Demonstrate ability to learn elementary ideas from number theory which will have applications in cryptography.
- 2. Introduce various cryptosystems and apply them in the necessary fields.
- 3. Understand the concepts of public key and primality
- 4. Learn the public key cryptography and RSA algorithm
- 5. Get the knowledge about Factoring concepts.

Course Outcomes:

After successful completion on the course the student will be able to

- **CO1** Acquire the knowledge of elementary number theory
- **CO2** Apply various cryptosystems and understand the concepts of quadratic, residues and reciprocity
- CO3 Develop the idea of public key cryptography, RSA Algorithms.
- **CO4** Solve problems using the continued fraction method and the quadratic sieve method.
- **CO5** Demonstrate ability to apply concepts of Fermat factorization and factor bases.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	No

UNII-I	Some Topics in Elementary I	Number Theory	15 nours
Time Estimates	for doing arithmetic – Divisibil	ity and Euclidean Algorithm - Congru	ence's- Some
applications to H	Factoring.		
Chapter I			
UNIT–2	Cryptography		15 hours
Some simple cr	ptosystems – Enciphering matri	ices.	
Chapter III			

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15 hours

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Quadratic Residues Quadratics - Residues and reciprocity.

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Chapter II

UNIT-3

TINIT/D 4

UNIT-4 Public Key										15	15 hours			
The	idea	of	Public	key	Cryptography	_	RSA	_	Discrete	Law	_	Knapsack	_	Zero-

Knowledge. Chapter IV: Sections 1 to 5

UNIT-5 **Primality and Factoring** 15 hours Pseudo-primes - The rho method - Fermat factorization and factor bases - The continued fraction method – The quadratic sieve method.

Chapter V: Sections 1 to 5

Text Book:

Neal Koblitz, A Course in Number Theory And Cryptography, Springer-Verlag, New York,1987.

Reference Books:

- 1. Niven and Zuckerman, An Introduction to Theory of Numbers, Third Edition, Wiley Eastern Ltd, New Delhi, 1976.
- 2. David M. Burton, Elementary Number Theory, Wm. C. Brown Publishers, Dubuque, Iowa, 1989.
- 3. K. Ireland and M. Rosen, A Classical Introduction to Modern Number Theory, Springer-Verlag, 1972.

E-Materials:

- 1. http://mathworld.wolfram.com
- 2. https://ocw.mit.edu/courses/6-042j-mathematics-for-computer-science-fall-2010/resources/lecture-4-number-theory-i/

93

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	S	Μ	Μ	Μ	S	S	S	S
CO2	S	S	S	Μ	Μ	S	S	S	S	S
CO3	S	S	S	Μ	S	S	S	S	S	S
CO4	S	S	S	Μ	S	S	S	S	S	S
CO5	S	S	S	Μ	S	Μ	S	S	S	S

Mapping with Learning outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV	Paper type : Core Elective	Credit	:	3
Paper code :	Name of the Paper : AdvancedNumericalAnal	ysis		
Hours of Teaching: 75hrs				

CourseObjectives:

The main objective of this course are to:

- 1 Introducethederivationofnumericalmethodswitherroranalysis
- 2 Studythetranscendental andpolynomialequations
- 3 Acquire the knowledge of systemoflinear algebraic equations
- 4 Understandthedifferentiationandintegration
- 5 Solve problems on interpolation and ordinary differential equations

CourseOutcomes:

Aftersuccessful completion of the course the student will be able to

- CO1 Examine the solutions of transcendental and polynomial equations
- CO2 Understandthesystem of linear algebraic equations
- **CO3**Analyse the interpolationandextrapolation
- CO4 Evaluatenumerical differentiation and integrations
- CO5 Solve the differential equations by single and multi stepmethods

Matching Table:

Unit	Remembering	Understanding	nderstanding Applying A		Analyzing Evaluating	
1	Yes	Yes	No	No	Yes	No
2	Yes	Yes	No	No	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	No	No	Yes	No
5	Yes	Yes	Yes	Yes	Yes	Yes

UNIT-1 **TranscendentalandPolynomialEquations** Iterationmethodsbasedonseconddegreeequation-Rateofconvergence-Iterationmethods-Methods forcomplexroots-Polynomial equations. Chapter2:Sections 2.4 to 2.8

UNIT-2 Systemof LinearAlgebraicEquations and Eigen 15hours **ValueProblems**

Directmethods-Triangularisation, Cholesky and Partition methods-Erroranalysis-Iteration methods -Eigen values and Eigenvectors – Jacobi's method, Given's method, Rutishaughermethodand Power method.

Chapter3: Sections 3.2to 3.5

UNIT-3 InterpolationandApproximation

HermiteInterpolations-PiecewiseandSplineInterpolation-Bivariateinterpolation-Approximation-Least Squareapproximation- Uniform approximation.

Chapter4:Sections4.5to 4.10

UNIT-4 DifferentiationandIntegration **15hours**

NumericalDifferentiation-PartialDifferentiation-NumericalIntegrationmethodsbasedonundetermined coefficients- Doubleintegration.

Chapter5:Sections5.2,5.5, 5.6, 5.8, 5.11

UNIT-5 **OrdinaryDifferential Equations** 15hours

Numericalmethods-Singlestepmethods-Multistepmethods-Predictor-Correctormethods.

Chapter6:Sections6.2 to 6.5

Text Book:

M.K.Jain, S.R.K.Iyengarand R.K.Jain, Numerical Methods For Scientificand Engineering Comput ation, 3rdEdition, New AgeInternational, 1993.

ReferenceBooks:

1. S.D.CorteanddeBoor,ElementaryNumericalAnalysis-

AnAlgorithmicapproach, 3rdEdition, McGrawHillInternationalBookCompany, 1980.

- JamesB.Scarboraugh, Numerical Mathematical Analysis, Oxford& IBHPublishing Compa 2. ny,New Delhi.
- F.B.Hildebrand, IntroductionToNumericalAnalysis, McGrawHill, NewYork, 1956. 3.

96

15hours

15hours

E-Materials:

- 1. <u>https://www.math.upenn.edu/~wilf/DeturckWilf.pdf</u>
- 2. <u>https://web.archive.org/web/20120225082123/http://kr.cs.ait.ac.th/~radok/math/mat7/stepsa.htm</u>
- 3. <u>https://ocw.mit.edu/courses/mechanical-engineering/2-993j-introduction-to-numerical-analysis-for-engineering-13-002j-spring-2005/</u>

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	Μ	S	S	S	S	S	Μ	S
CO2	S	S	Μ	Μ	S	S	S	S	Μ	Μ
CO3	S	S	Μ	S	S	S	S	S	Μ	S
CO4	S	S	S	Μ	Μ	S	S	S	Μ	Μ
CO5	S	S	Μ	Μ	S	S	S	S	Μ	S

Mapping with Learning outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115 M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV	Paper type : Core Elective	Credit	:	3	
Paper code :	Name of the Paper : Calculusof Variationand Equations	lIntegral			
Hours of Teaching: 75hrs					

Course Objectives:

The main objectives of this course are to:

- 1. Understand the conceptof calculus of variation and its applications.
- 2. Introduce the various types of integral equations.
- 3. Solve variational problems with fixed and moving boundaries.
- 4. Studythemethodsofsuccessiveapproximationsand Fredholmtheory.
- 5. AcquireknowledgeonapplicationstoOrdinaryDifferentialEquations.

Course Outcomes:

After successful completion of the course the student will be able to

- **CO1** Analyze the methods for variational problems with fixed boundaries.
- **CO2** Apply and solve the variational problems with moving boundaries.
- **CO3** Define the methods to solve integral equations.
 - CO4 Discuss the method of successive approximation and Fredholmtheory.
 - **CO5** Identify and Construct the solutions for real time applications.

Matching table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	No	Yes	Yes	No	Yes	No
2	No	Yes	Yes	Yes	Yes	Yes
3	Yes	Yes	Yes	No	Yes	No
4	No	Yes	Yes	Yes	Yes	No
5	Yes	Yes	Yes	Yes	Yes	Yes

Unit-I:VariationalProblemswith FixedBoundaries

The conceptofVariationand its properties – Euler'sequation– Variationalproblems forfunctionalsoftheform–Functionalsdependentonhigherorderderivatives–Functionalsdependent on Functions of several independent variables– Variational problem in parametricform– Someapplications to problems of mechanics.

Book-1: Chapter1:Sections 1.1 to 1.7

$\label{eq:unit-II:VariationalProblems with Moving Boundaries$

VariationalproblemwithaMovableboundaryforafunctionaldependentontwofunctions– Onesidedvariations–ReflectionandRefractionofextremals–Diffractionoflightrays.

Book-1:Chapter2: Sections 2.2 to 2.5

Unit–III:IntegralEquations

Introduction– Definition–Regularity conditions– Special kindsof Kernels– Eigen valuesand Eigen functions – Convolution integral – Reduction to a system of algebraic equations –Examples– Fredholmalternative–Examples–Anapproximationmethod.

Book-2:Chapter1: Sections 1.1 to1.5

Chapter2: Sections 2.1 to 2.5

Unit-IV:MethodofSuccessiveApproximationsandFredholmTheory

hoursMethodofsuccessiveapproximations–Iterativescheme–Examples–Volterraintegralequations– Examples–Someresultsabouttheresolventkernel–ThemethodofsolutionofFredholmequation– Fredholmfirsttheorem–Examples.

Book-2:Chapter3:Sections3.1 to3.5

Chapter4: Sections:4.1 to 4.3

Unit-V: Applications to Ordinary Differential Equations

Initialvalueproblems–Boundary valueproblems–Examples–Singularintegralequations –TheAbelintegralequations-Examples.

Book-2:Chapter5:Sections5.1to5.3

Chapter8:Sections8.1to8.2

Text Books:

- 1. A.S.Gupta, Calculus of Variations with Applications, PHI, New Delhi, 2005.
- 2. Ram P.Kanwal, *Linear Integral Equations*, Theory and Techniques, Academic Press, New York, 1971.

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ReferenceBooks:

- 1. M.D.Raisinghania, *IntegralEquationsandBoundaryValueProblems*, S.Chand&Co., NewDelhi, 2007.
- 2. SudirK.PundirandRimplePundir,*IntegralEquationsandBoundaryValueProblems*,PragatiPrak asam, Meerut.2005.

E–Materials:

- 1. <u>http://www.maths.ed.ac.uk/~jmf/Teaching/Lectures/CoV.pdf</u>
- 2. https://archive.nptel.ac.in/courses/111/104/111104025/

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	М	S	S	М	М	S
CO2	S	S	S	М	S	S	S	М	М	S
CO3	S	S	М	М	М	М	S	М	S	М
CO4	S	S	S	S	S	М	S	М	S	М
CO5	S	S	S	М	S	М	S	М	S	М

Mapping with Learning outcomes:

* PO – Programme Outcome, CO – Course Outcomes

THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IVPaper type : Open ElectiveCredit : 3Paper code :Name of the Paper : Mathematical Economics

Hours of Teaching: 75hrs

CourseObjectives:

Themain objectives of the course are to

- 1. Provide basic knowledge of the origin of theoryofFIRM
- 2. Study the CES Production Function
- 3. Develop the PerfectCompetition
- 4. understandabout market equilibrium
- 5. Discuss the WelfareEconomics

CourseLearningOutcomes

Afterthesuccessful completion of this course, the students will be able to

- **CO1** understand the knowledgeof FIRM theoryandperfectcompetition
- CO2 Analyzethe CESproduction
- CO3 To acquire the knowledge of market equilibrium
- **CO4** To control thestability of equilibrium
- CO5 Discuss thewelfareeconomics, taxes and subsidies

Matching Table:

Unit	Remembering	Understanding	erstanding Applying		Evaluating	Creating
1	Yes	Yes	No	Yes	Yes	No
2	Yes	Yes	Yes	Yes	Yes	No
3	Yes	Yes	Yes	Yes	Yes	No
4	Yes	Yes	Yes	Yes	Yes	Yes
5	Yes	Yes	Yes	Yes	Yes	Yes

Unit-1:TheTheory of FIRM

Basic Concepts - Optimizing Behavior - Input Demands - Cost Functions – Joint Products - Generalizationto m variables.

Chapter4: Sections 4.1 to 4.6

Unit-2:CESProduction

Homogeneous Production functions – CES Production Function.

Chapter5: Sections5.1 and 5.2

Unit-3:PerfectCompetition

Assumptions of Perfect Competition - Demand Functions - Supply Functions –Commodity-Market Equilibrium-An application to Taxation.

Chapter6: Sections 6.1to 6.5

Unit-4:MarketEquilibrium

Factor-Market Equilibrium - Existence and Uniqueness of Equilibrium - Stability of Equilibrium-DynamicEquilibrium withLaggedAdjustment.

Chapter6: Sections 6.6to 6.9

Unit-5:WelfareEconomics

Pareto Optimality - the efficiency of Perfect competition - The efficiency of Imperfectcompetition -External Effects in consumption and Production - Taxes and Subsidies –SocialWelfarefunctions-Thetheoryof SecondBest.

Chapter11: Sections 11.1 to 11.7

Text Book:

JamesM.HendersonandRichard

E.Quandt,MicroEconomicTheoryAMathematicalApproach,(3rdEdn.)TataMcGrawHill,NewD elhi,2003.

ReferenceBooks

- William J. Baumol. Economic Theory and Operations Analysis, Prentice Hall ofIndia, NewDelhi, 1978
- A.C.Chiang, Fundamental Methods of Mathematical Economics, McGraw Hill, NewYork, 1984
- 3. Michael D. Intriligator, Mathematical Optimization and Economic Theory, PrenticeHall, New York, 1971.

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4. A.Kautsoyiannis, Modern Microeconomics (2ndedn) MacMillan, New York, 1979

E–Materials:

- 1. <u>https://curlie.org/Science/Math/Applications/Mathematical_Economics_and_Financial_Math</u> <u>ematics/</u>
- 2. <u>http://master-economics-qem.univ-paris1.fr/about/?no_cache=1</u>

Mapping with Learning Outcomes:

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	Μ	S	S	Μ	S	Μ	S	L	S	L
CO2	Μ	L	Μ	S	L	S	Μ	S	L	Μ
CO3	S	S	L	S	S	L	S	S	Μ	L
CO4	S	S	Μ	L	Μ	Μ	S	Μ	L	S
CO5	Μ	L	Μ	S	L	Μ	Μ	S	L	Μ

* PO – Programme Outcome, CO – Course Outcomes
THIRUVALLUVAR UNIVERSITY, VELLORE – 632115

M.Sc. Mathematics – 2022 - 2023 onwards

Semester : IV	Paper type : Open Elective	Credit	:	3
Paper code :	Name of the Paper : Entrepreneurial Develop	ment		
Hours of Teaching: 75hrs				

Course Objective:

The objectives of this course are to

- 1 Provideanunderstandingofbasicconceptintheareaof entrepreneurship
- 2 Exposestudentstotheideageneration,creatingawarenessofbusinessopportunities,andfami liarizingthemwith formal practices ineffective project formation.
- 3 Understand an ProjectManagementandIdeaGeneration
- 4 Develop the NationalInstitute of Entrepreneurship and Small Business Development
- 5 Discuss the PMEGP– NEEDS– UYEGP

CourseLearningOutcomes

Afterthesuccessful completion of this course, the students will be able to

- CO1 Understandtheknowledgeofentrepreneurship
- CO2 Develop the EntrepreneurialDevelopment
- CO3 Analyze the entrepreneurial finance and role of various government agencies
- CO4 Develop the idea generation, creating awareness of business opportunities, and familiarizing them with formal practices
- **CO5** Discuss the Government Policies and benefits.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating	
1	Yes	Yes	Yes	Yes	Yes	No	
2	Yes	Yes	Yes	Yes	Yes	No	
3	Yes	Yes	Yes	Yes	Yes	No	
4	Yes	Yes	Yes	Yes	Yes	Yes	
5	Yes	Yes	Yes	Yes	Yes	Yes	

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Unit-1:Introduction

EntrepreneurandEntrepreneurship–Concept–Definition-ClassificationofEntrepreneurWomen Entrepreneur - Functions of an Entrepreneur - Traits of successful Entrepreneur -EntrepreneursVsProfessionalManagers–RoleofanEntrepreneurinEconomicDevelopment-Future challenges.

Unit-2:EntrepreneurialDevelopment

hoursEntrepreneurialDevelopmentProgrammes–Meaning-EvolutionandObjectivesofEDP-InstitutionaleffortstodevelopEntrepreneurship-NationalSkillDevelopmentCorporation(NSDC)-RoleofGovernment inOrganisingEDPs-Operational ProblemofEDPs.

Unit-3:ProjectManagementandIdeaGeneration

hoursProjectManagement-ProjectIdentification-ProjectFormulation-ProjectDesignandNetworkAnalysis–OverviewofProjectAppraisal-ProjectReport-IdentificationandSelectionofBusinessOpportunity–IdeaGeneration– OverviewofTechniquesusedforIdeaGeneration.-Individual creativity.

Unit-4:EntrepreneurialFinanceandDevelopmentAgencies

hoursSourcesofFinance-CommercialBanksandDevelopmentBanks-

RoleofAgenciesinassistingEntrepreneurship-

DistrictIndustriesCenters(DIC),SmallIndustriesServiceInstitute(SISI),EntrepreneurshipDevelopmentInstituteofIndia(EDII),NationalInstituteofEntrepreneurship &Small

BusinessDevelopment(NIESBUD), NationalEntrepreneurshipDevelopment Board(NEDB).

Unit-5:Government PoliciesandBenefits

TaxBenefits–TaxHolidays–AllowancefordeductingDepreciation–RehabilitationAllowance–Benefits available forMSMEs: PMEGP– NEEDS– UYEGP.

Text Books:

- 1. Dr.S.S.Khanka,EntrepreneurshipDevelopment- S. Chand&Co.,NewDelhi.
- 2. JayashreeSuresh,EntrepreneurialDevelopment, MarghamPublication,Chennai.
- 3. VasantDesa,Dynamics ofEntrepreneurialDevelopment–HimalayaPublication.
- 4. RobertD.Hisrich,MichaelP.Peters&DeanA.Shepherd,Entrepreneurship, TataMcGraw Hill PublishingCompanyLimited, New Delhi.
- 5. RavindranathV.Badi&Narayana,Entrepreneurship,VrindaPublication(P)Ltd,New Delhi.

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ReferencesBooks:

- 1. RabindraN.Kanungo,EntrepreneurshipandInnovation,SagePublications,NewDelhi.
- 2. HoltD.H.,EntrepreneurshipNewVentureCreation.NewDelhi:PrenticeHallofIndia.
- 3. HisrichR, and Peters, M., Entrepreneurship. New Delhi: TataMcGrawHill.
- 4. RajkonwarA.B.,Entrepreneurship,KalyaniPublisher, Ludhiana.
- 5. Charantimath,Poornima,EntrepreneurshipDevelopmentandSmallBusinessEnterprises,Pearso n Education, New Delhi.

E-Materials:

- 1. <u>http://www.indcom.tn.gov.in/pmegp.html</u>
- 2. <u>http://www.indcom.tn.gov.in/needs.html</u>
- 3. <u>http://www.indcom.tn.gov.in/uyegp.html</u>

COs **PO1 PO2 PO3 PO4 PO5 PO6 PO7 PO8 PO9 PO10 CO1** L S Μ S Μ S Μ S Μ S **CO2** Μ Μ Μ S S L Μ S L Μ **CO3** S Μ S S L L S L Μ L **CO4** S S L Μ Μ Μ S L S Μ **CO5** S S Μ L S Μ L L S Μ

Mapping with Learning Outcomes:

* PO – Programme Outcome, CO – Course Outcomes

* S – Strong, M – Medium, L – Low

THIRUVALLUVAR UNIVERSITY, VELLORE – 632 115 M.Sc. Mathematics – 2022-2023 Onwards

Semester : IVPaper Type : Open ElectiveCredit : 3Paper Code :Name of the Paper : Programming in C++Hours of Teaching: 75hrs

Course Objectives

The objectives of this course are to

- 1. Introduce the tokens expressions and control structures in C++.
- 2. Explore the usage of all basic functions in C++.
- 3. Educate the significance of various types of classes in C++.
- 4. Inculcate the inheritance structures in C++.
- 5. Indoctrinate the polymorphism concepts in C++.

Course Outcomes

After the successful completion of this course, the students will be able to

- **CO1** Know the tokens expressions and control structures in C++.
- CO2 Understand the usage of all basic functions in C++.
- CO3 Comprehend the significance of various types of classes in C++.

CO4 Acquire the knowledge about the inheritance structures in C++.

CO5Apply the polymorphism concepts in C++.

Matching Table:

Unit	Remembering	Understanding	Applying	Analyzing	Evaluating	Creating
1	Yes	Yes	Yes	No	No	No
2	Yes	Yes	Yes	No	No	No
3	Yes	Yes	Yes	Yes	No	No
4	Yes	Yes	Yes	Yes	No	No
5	Yes	Yes	Yes	Yes	No	No

Unit-1 : Tokens Expressions and Control Structures

Tokens - Keywords - Identifiers and Constants - Basic Data Types - Uses Defined Data Types – Derived Data Types – Symbolic – Operators in C++ – Scope Resolution Operator – Manipolators - Operator Overloading - Control Structures. **Chapter 3:** Sections 3.1 – 3.24

Unit-2 : Functions

Characteristic of OOP - Function Prototype - Default Arguments - Inline Functions -Function Overloading – Template Functions.

Chapter 4: Sections 4.2, 4.3, 4.6, 4.7, 4.9

Unit-3 : Classes in C++

Classes - Constructors and Destructors - Friend functions - Template Classes - New and Delete Operators - Operator Overloading.

Chapter 5: Sections 5.1 - 5.15

Chapter 6: Sections 6.1 – 6.9

Chapter 7: Sections 7.1 - 7.5

Unit-4 : Inheritance

Single Inheritance - Multiple Inheritance - Hierarchical Inheritance - Hybrid Inheritance -Virtual Functions.

Chapter 8: Sections 8.1 - 8.8

Unit-5: **Polymorphism in C++**

Polymorphism.

Chapter 9: Sections 9.6 – 9.7

Text Books:

E. Balagurusamy, *Object Oriented Programming with C++*, 4thEdn., Tata McGraw Hill Publishing Company Ltd., New Delhi, 2001.

Reference Books:

- 1. E. Balagurusamy, Numerical Methods, Tata McGraw Hill Publishing Company Ltd., New Delhi,1999.
- 2. John H. Mathews, Numerical Methods for Mathematics, Science and Engineering, 2ndEdn., Prentice Hall India Pvt. Ltd., 2003.

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- 3. S.S. Sastry, Introductory to Numerical Methods, Prentice Hall India Pvt. Ltd., 2000.
- H.C. Saxena, *Finite Differences and Numerical Analysis*, S. Chand & Company Ltd., New Delhi, 2005.

E-Materials:

- 1. <u>https://onlinecourses.nptel.ac.in/noc21_cs02/preview</u>
- 2. https://www.cet.edu.in/noticefiles/285_OOPS%20lecture%20notes%20Complete.pdf
- 3. <u>https://www.msuniv.ac.in/images/e-</u> content/1.Object%20Oriented%20Programming%20with%20C%20and%20Java.pdf

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10
CO1	S	S	М	М	S	S	S	S	S	S
CO2	S	S	М	М	S	S	S	S	S	S
CO3	S	S	М	М	S	S	S	S	S	S
CO4	S	S	М	М	S	S	S	S	S	S
CO5	S	S	М	М	S	S	S	S	S	S

Mapping with Programme Outcomes:

*PO – Programme Outcome, CO – Course Outcome.

*S – Strong, M – Medium, L – Low.